

# Particle-based Viscoelastic Fluid Simulation

Simon Clavet, Philippe Beaudoin, Pierre Poulin

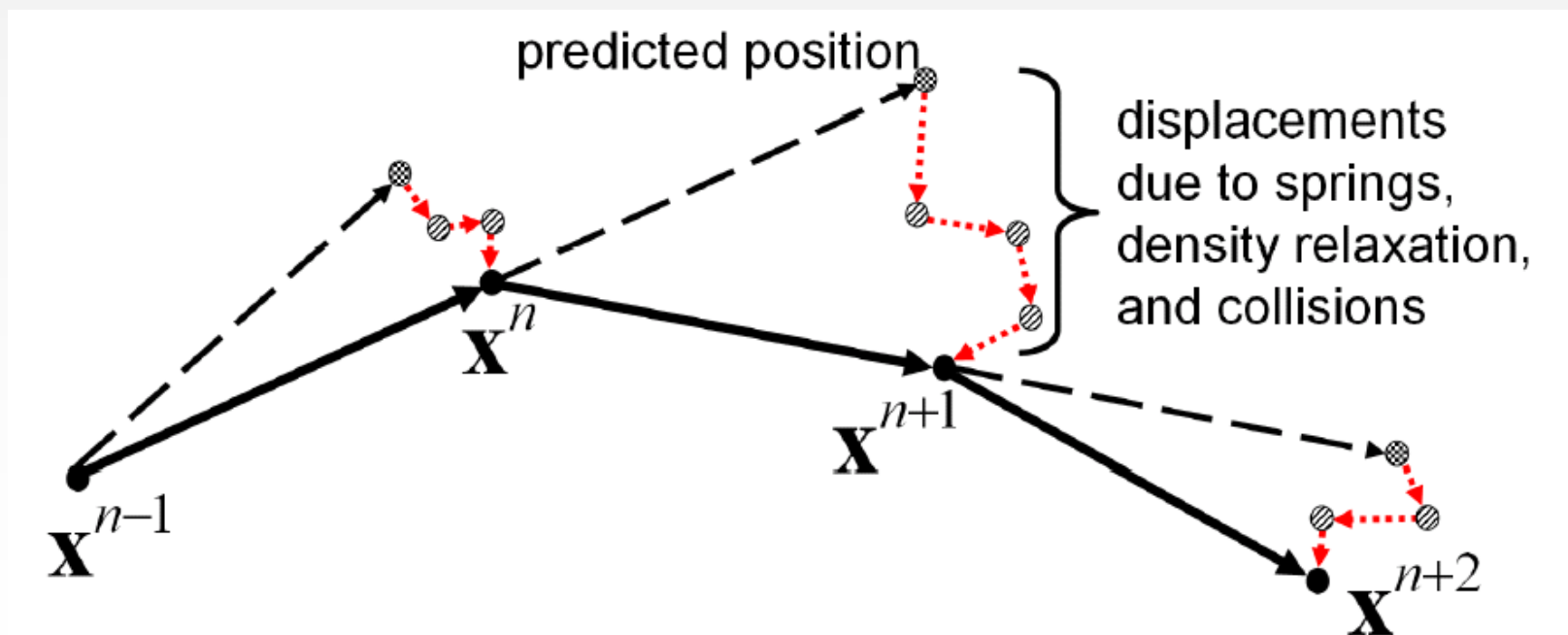
**Jaroslav Budiš**

# Goals

- Intuitive and versatile framework for particle-based fluid simulation
- Viscoelasticity
  - Viscosity
  - Elasticity
- Plasticity
- Incompressibility
- Stickiness

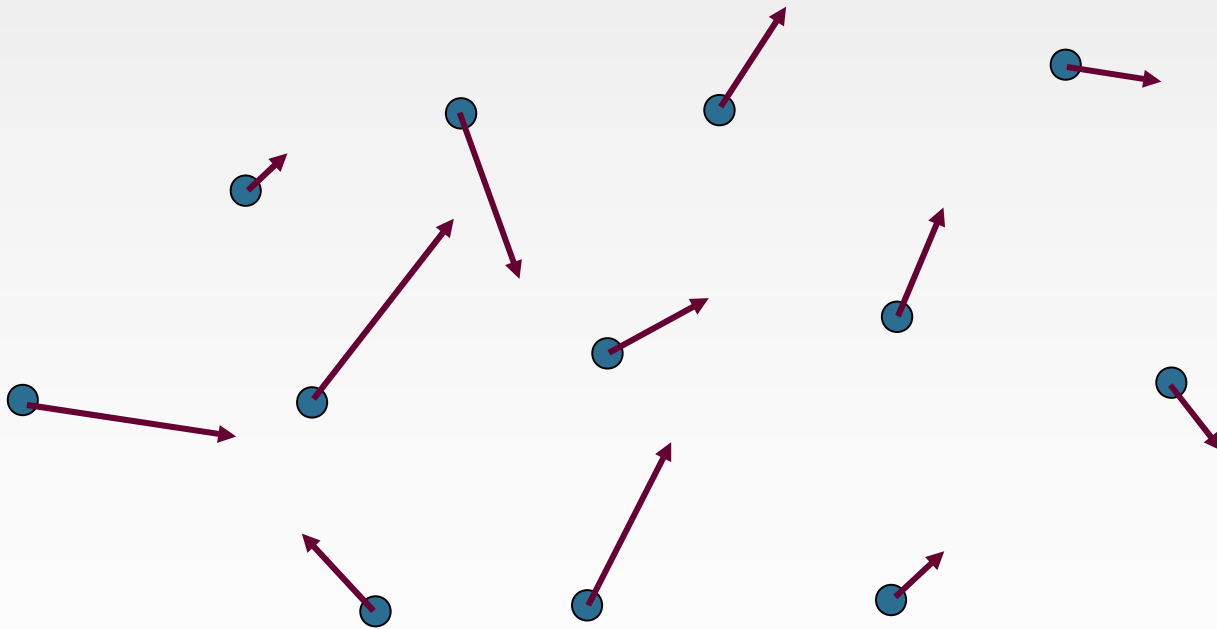
# Integration scheme

- Advance particles to predicted positions
- Relax according to positional constraints



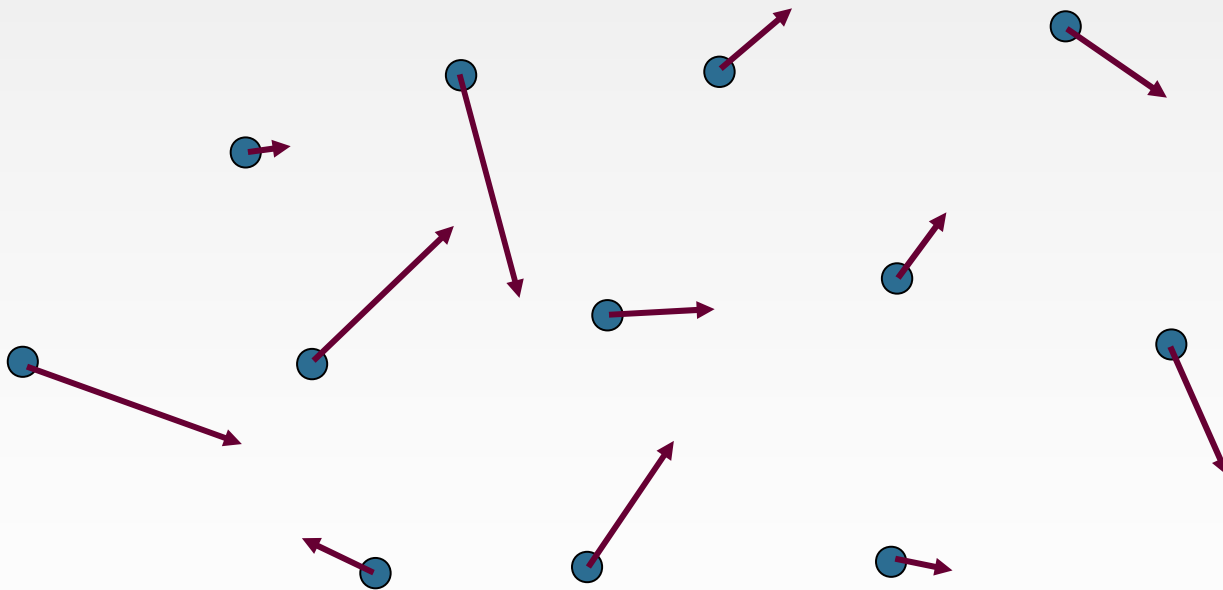
# Simulation

- Preserved velocities



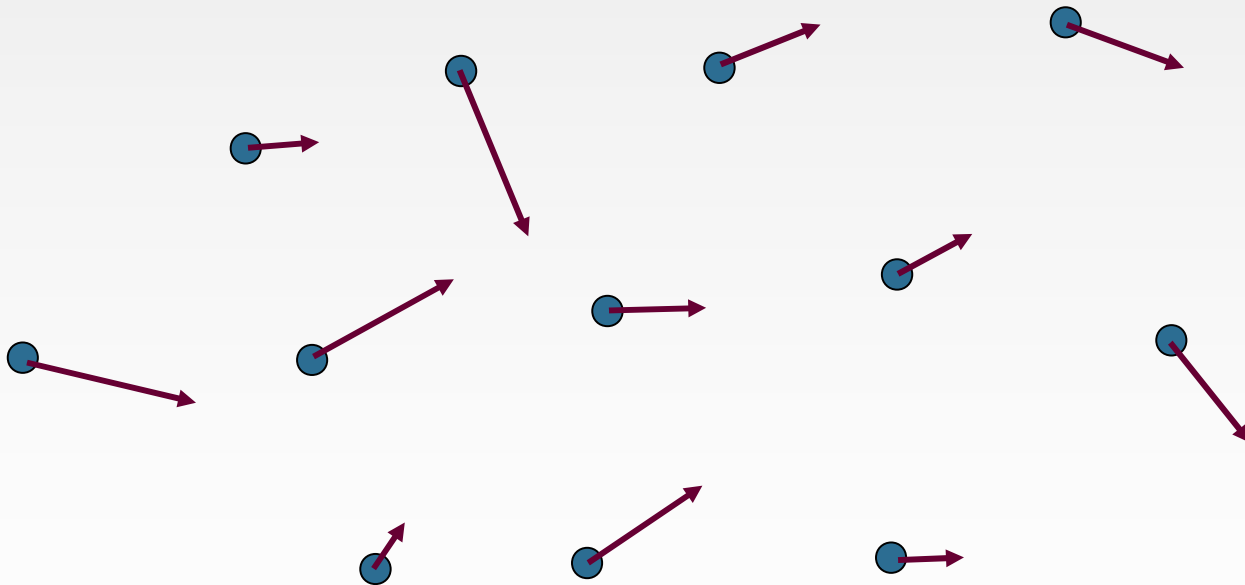
# Simulation

- Apply gravity



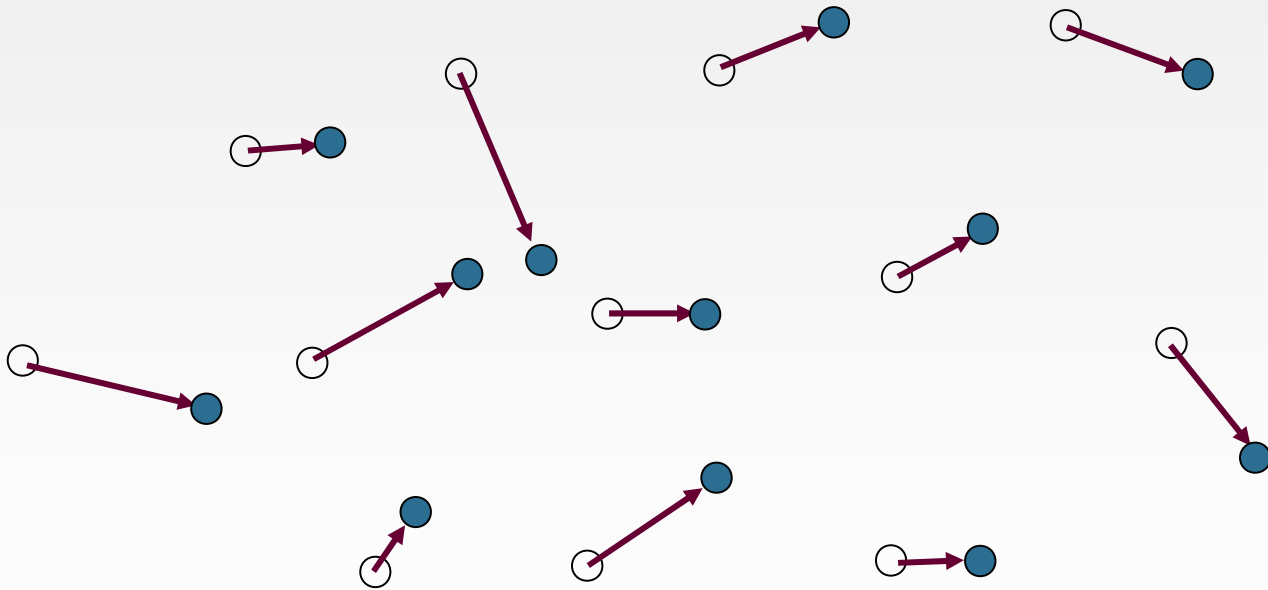
# Simulation

- Apply viscosity



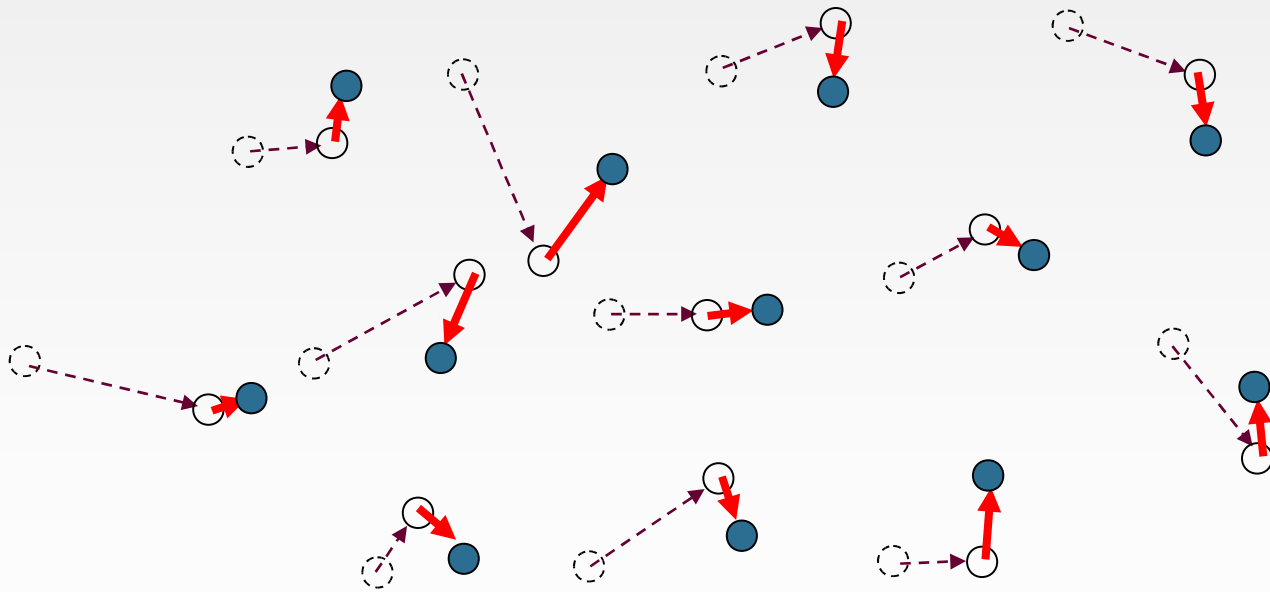
# Simulation

- Advance to predicted positions



# Simulation

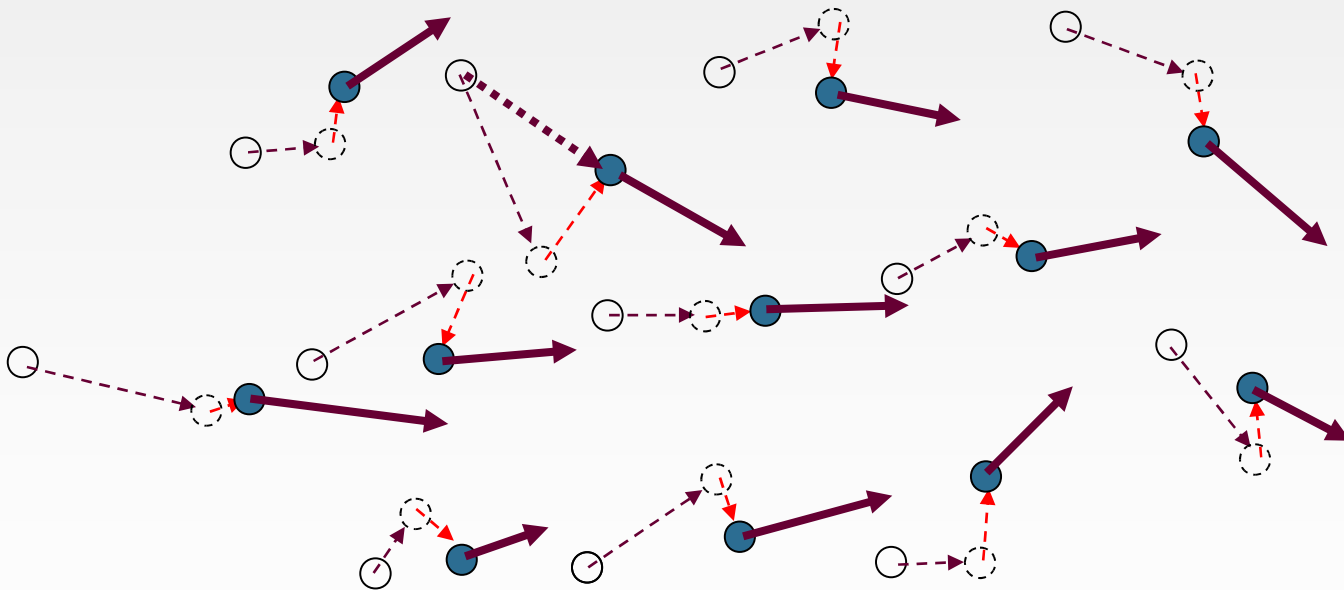
- Relax (density and strings)





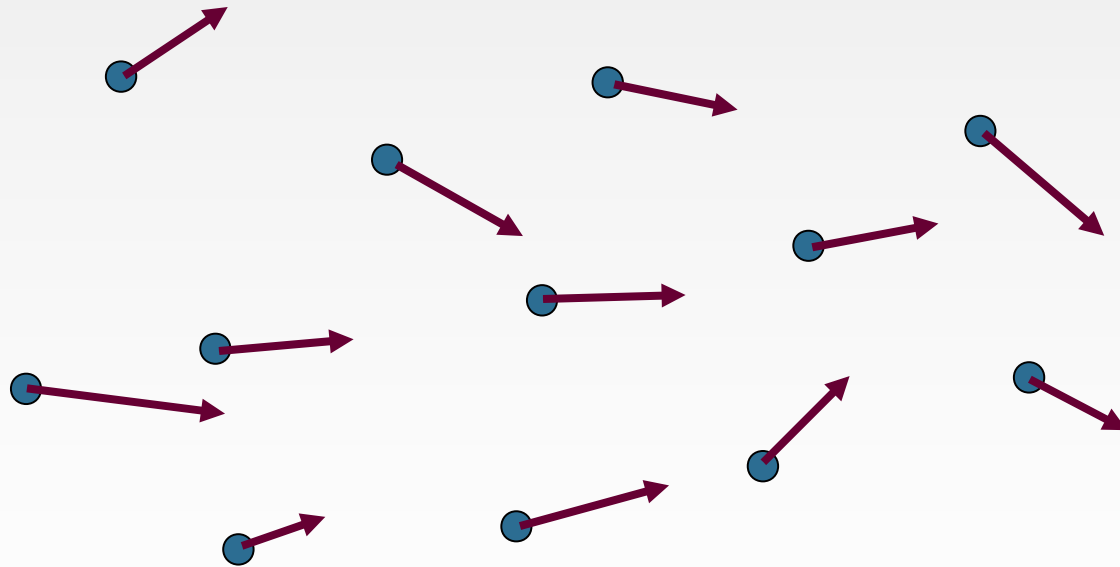
# Simulation

- Obtain new velocities



# Simulation

- Repeat with new velocities



# Density relaxation

- Goal
  - Minimize compressibility
  - Maintain constant density
- Approach
  - For each particle
    - Compute its density
    - Modify particle and its neighbors position to approach rest density

# Initialization

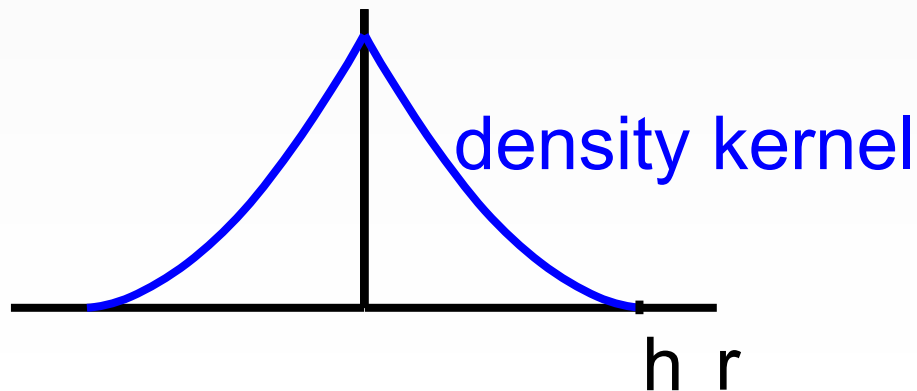
- For each particle

- Compute density

$$\rho_i = \sum_{j \in N(i)} \left( 1 - \frac{r_{ij}}{h} \right)^2$$

- Compute proportional pressure

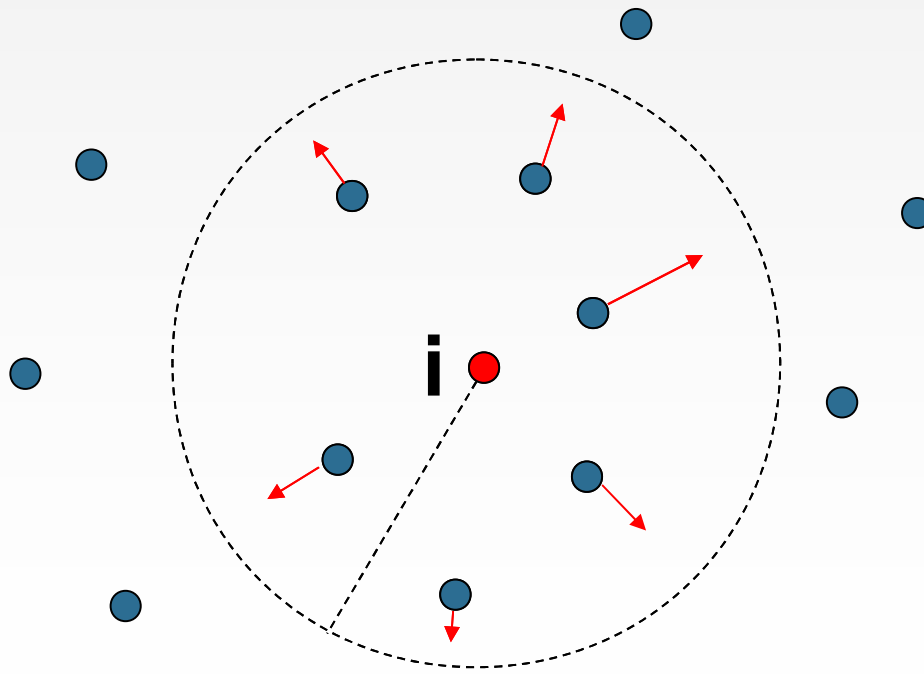
$$P_i \sim \rho_i - \rho_0$$



# Particles relocation

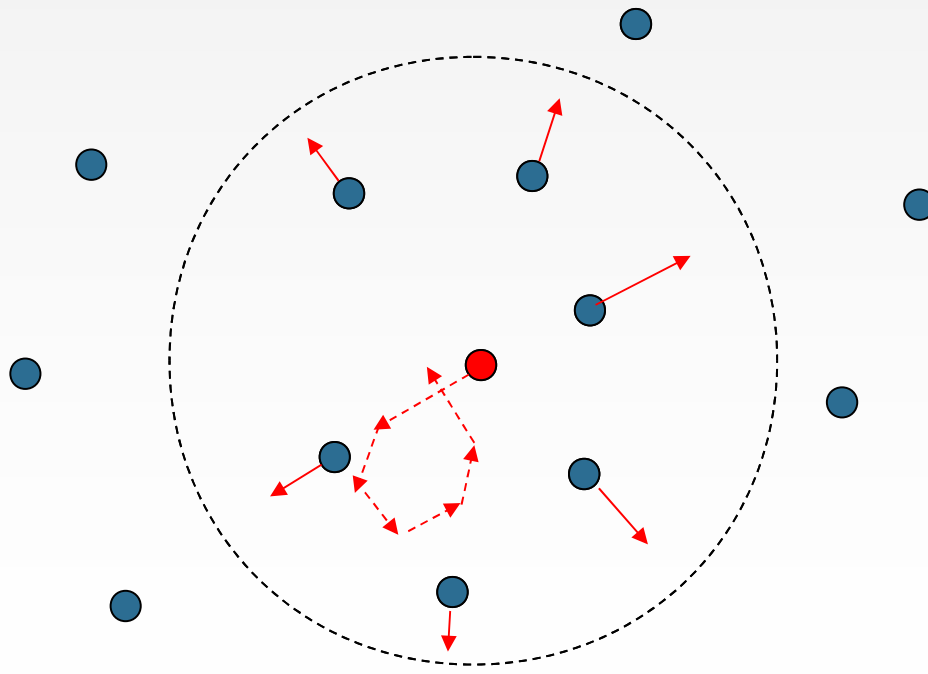
- Compute displacement for neighbors

$$D \sim P_i \left( 1 - \frac{r_{ij}}{h} \right)$$



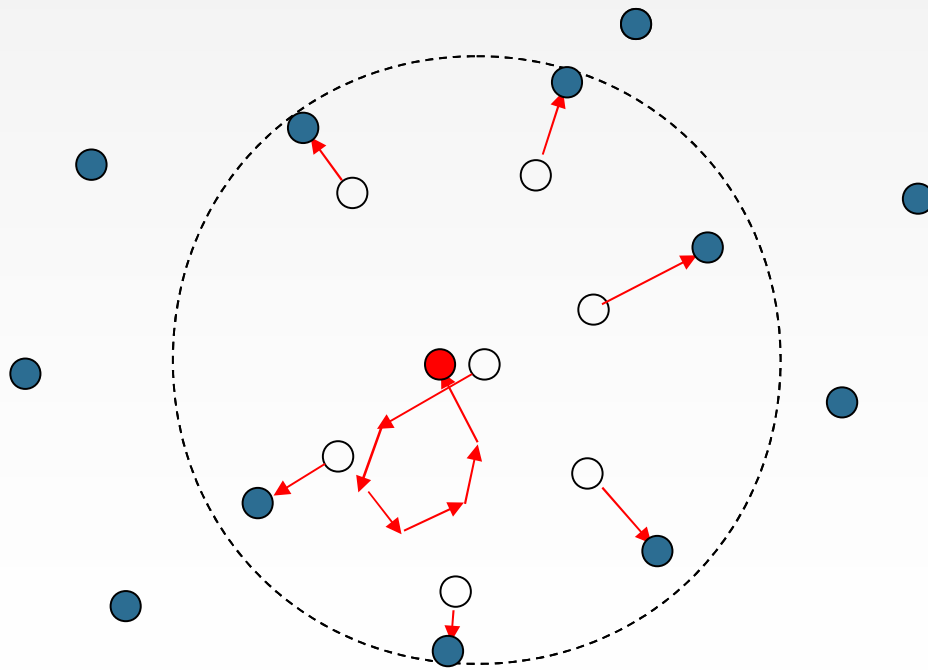
# Particles relocation

- Compute displacement for particle



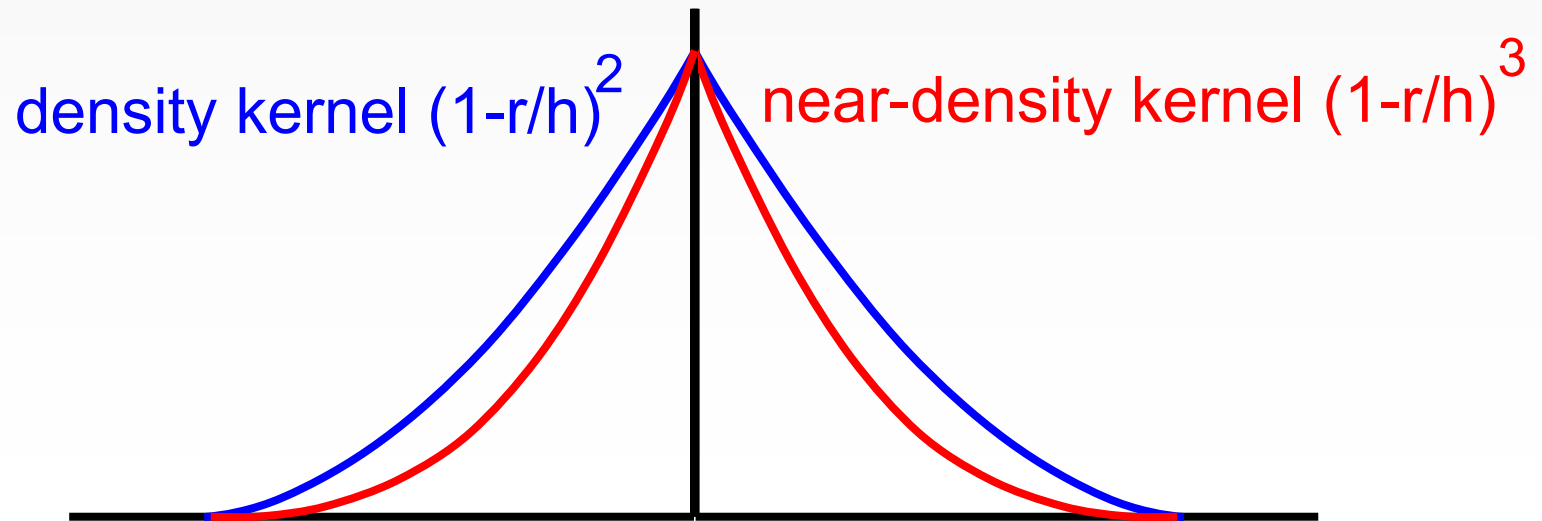
# Particles relocation

- Move particles



# Near-density

- Motivation
  - Avoid particle clustering
- Solution
  - Add repulsive forces for near neighbors
  - Sharper near-density kernel





# Near-density

- Near-density has zero rest value (only repulsive forces)

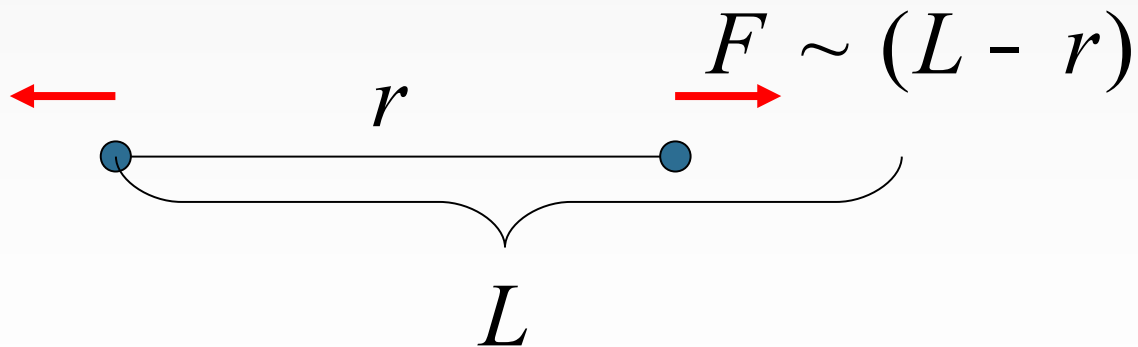
- Density  $P_i \sim \rho_i - \rho_0$

- Near-density  $P_i^{NEAR} \sim \rho_i^{NEAR}$

- Neighbor displacement  $D \sim P_i \left( 1 - \frac{r_{ij}}{h} \right) + P_i^{NEAR} \left( 1 - \frac{r_{ij}}{h} \right)^2$

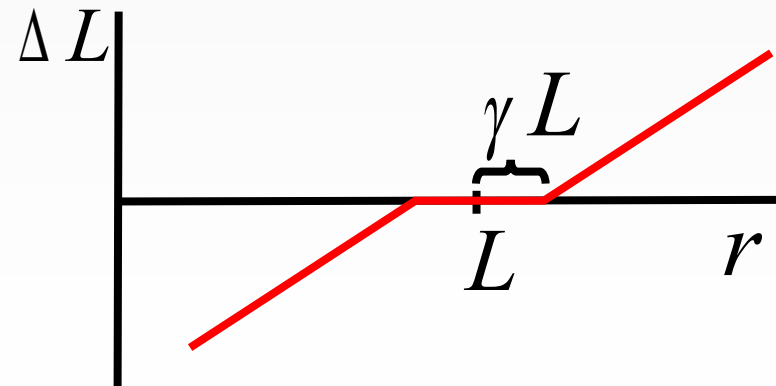
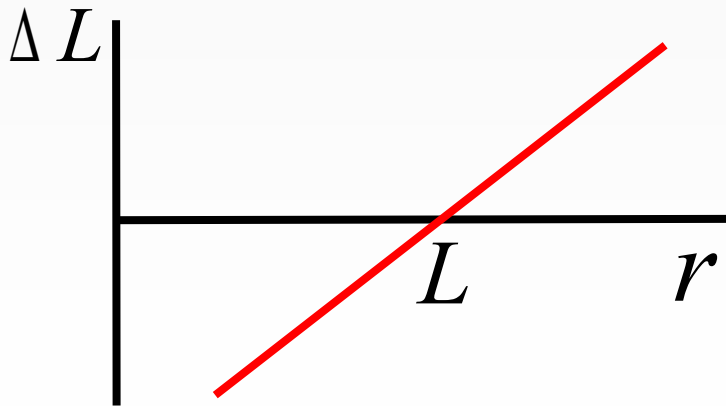
# Elasticity

- Springs between neighboring particles
- Move particles to achieve spring rest length

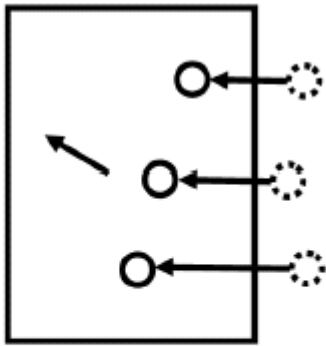


# Plasticity

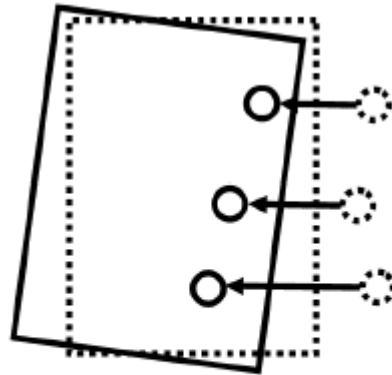
- Add and remove strings
- Change string rest length based on current length
- Linear
  - Plastic flow for every deformation  $\Delta L \sim \alpha (r - L)$
- Nonlinear
  - Plastic flow only if deformation is large enough



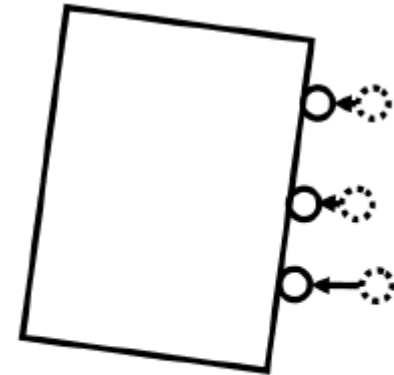
# Collisions



1) Accumulate particle impulses on body



2) Update body configuration



3) Update particle positions

# Stickiness

- Detach particles to objects
- Apply, if distance small enough
- Attraction impulse to particles

# Results

- Video

# Zdroje

- Particle-based Viscoelastic Fluid Simulation (Simon Clavet, Philippe Beaudoin, Pierre Poulin)
- <http://www.iro.umontreal.ca/labs/infographie/papers/Clavet-2005-PVFS/index.html>

# Priestor na otázky