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# Computer Graphics

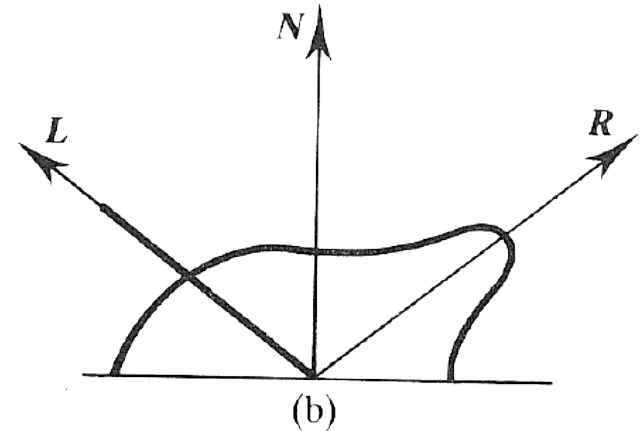
- Shading & Texturing -

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# Empirical BRDF Approximation

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- Purely heuristic model
  - Initially without units (values  $\in [0,1]$ )
- $L_r = L_{r,a} + L_{r,d} + L_{r,s}$  ( +  $L_{r,m}$  +  $L_{r,t}$  )
- $L_{r,a}$ : Ambient term
  - Approximate indirect illumination
- $L_{r,d}$ : Diffuse term (Lambert)
  - Uniform reflection
- $L_{r,s}$ : Specular term
  - Mirror-reflection on a rough surface
- $L_{r,m}$ : Perfect reflection
  - *Only possible with Ray-Tracing*
- $L_{r,t}$ : Perfect transmission
  - *Only possible with Ray-Tracing*



# Phong Illumination Model

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- **Extended light sources:  $l$  point light sources**

$$L_r = k_a L_{i,a} + k_d \sum_l L_l (I_l \cdot N) + k_s \sum_l L_l (R(I_l) \cdot V)^{k_e} \quad (\text{Phong})$$

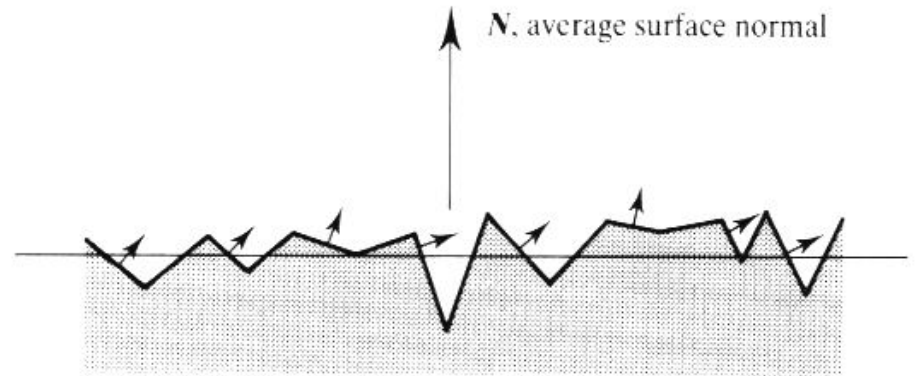
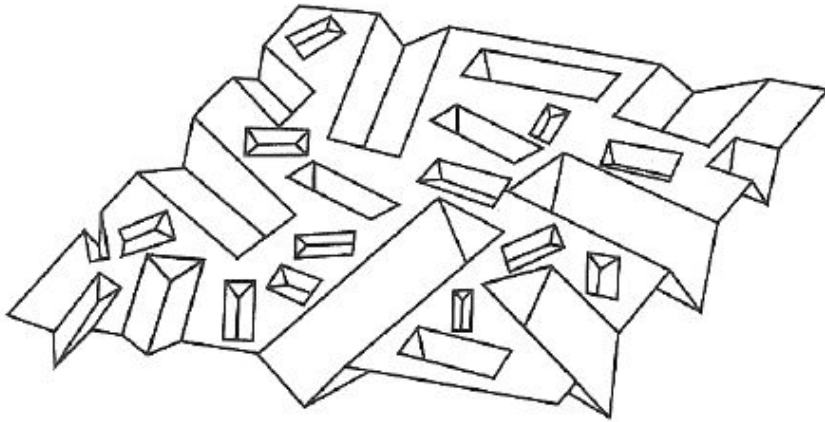
$$L_r = k_a L_{i,a} + k_d \sum_l L_l (I_l \cdot N) + k_s \sum_l L_l (H_l \cdot N)^{k_e} \quad (\text{Blinn})$$

- **Color of specular reflection equal to light source**
  - **Heuristic model**
    - Contradicts physics
    - Purely local illumination
      - Only direct light from the light sources
      - No further reflection on other surfaces
      - Constant ambient term
  - **Often: light sources & viewer assumed to be far away**
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# Microfacet Model

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- **Isotropic microfacet collection**
- **Microfacets assumed as perfectly smooth reflectors**
- **BRDF**
  - Distribution of microfacets
    - Often probabilistic distribution of orientation or V-groove assumption
  - Planar reflection properties
  - Self-masking, shadowing



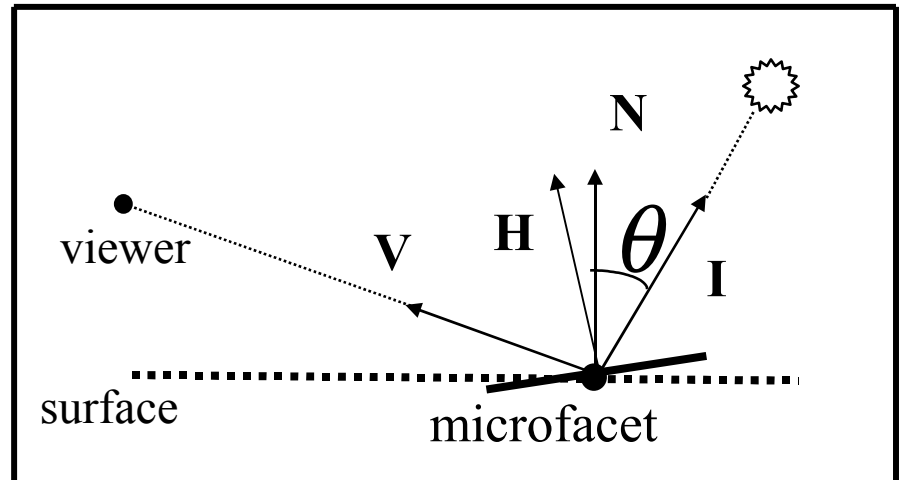
# Ward Reflection Model

- **BRDF**

$$f_r = \frac{\rho_d}{\pi} + \rho_s \frac{1}{\sqrt{(I \cdot N)(V \cdot N)}} \cdot \frac{\exp(-\tan^2 \angle(H, N) / \sigma^2)}{4\pi\sigma^2}$$

$\sigma$  standard deviation (RMS) of surface slope

- Simple expansion to anisotropic model ( $\sigma_x, \sigma_y$ )
- Empirical, not physics-based
- Inspired by notion of reflecting microfacets
- Convincing results
- Good match to measured data



# Physics-inspired BRDFs

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- **Notion of reflecting microfacet**
- **Specular reflectivity of the form**

$$f_r = \frac{D \cdot G \cdot F_\lambda(\lambda, \theta_i)}{\pi \underline{N} \cdot \underline{V}}$$

- D : statistical microfacet distribution
  - G : geometric attenuation, self-shadowing
  - F : wavelength, angle dependency of reflection along mirror direction
  - $\underline{N} \cdot \underline{V}$  : flaring effect at low angle of incidence
- **Cook-Torrance model**
    - F : wavelength- and angle-dependent reflection
    - Metal surfaces
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# Cook-Torrance Reflection Model

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- **Cook-Torrance reflectance model** is based on the *microfacet* model. The BRDF is defined as the sum of a diffuse and specular components:

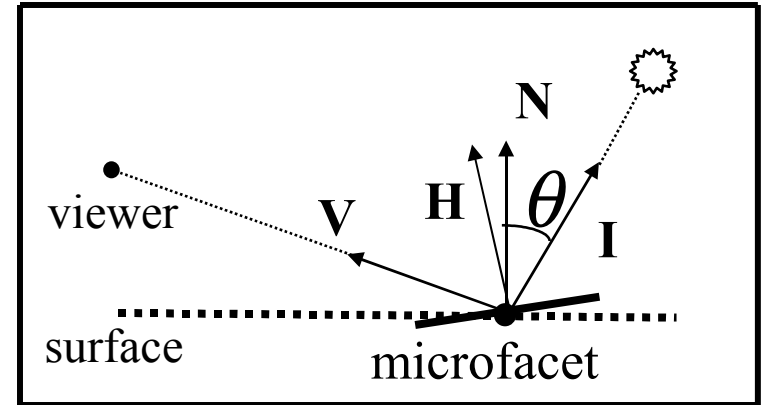
$$f_r = k_d \rho_d + k_s \rho_s; \quad k_d + k_s \leq 1$$

where  $k_s$  and  $k_d$  are the specular and diffuse coefficients.

- Derivation of the specular component  $\rho_s$  is based on a **physically derived** theoretical reflectance model
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# Cook-Torrance Specular Term

$$\rho_s = \frac{F_\lambda DG}{\pi(\underline{N} \cdot \underline{V})(\underline{N} \cdot \underline{I})}$$



- **D : Distribution function of microfacet orientations**
- **G : Geometrical attenuation factor**
  - represents self-masking and shadowing effects of microfacets
- **$F_\lambda$  : Fresnel term**
  - computed by Fresnel equation
  - relates incident light to reflected light for each planar microfacet
- **$\underline{N} \cdot \underline{V}$  : Proportional to visible surface area**
- **$\underline{N} \cdot \underline{I}$  : Proportional to illuminated surface area**



# Microfacet Distribution Functions

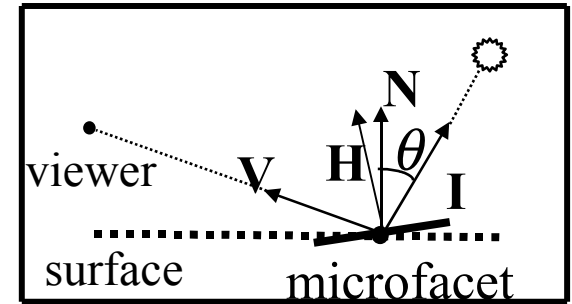
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- **Isotropic Distributions**  $D(\underline{\omega}) \Rightarrow D(\alpha)$   $\alpha = \mathbf{N} \cdot \mathbf{H}$

$\alpha$  : angle to average normal of surface

- Characterized by half-angle  $\beta$

$$D(\beta) = \frac{1}{2}$$



- **Blinn**

$$D(\alpha) = \cos^{\frac{\ln 2}{\ln \cos \beta}} \alpha$$

- **Torrance-Sparrow**

$$D(\alpha) = e^{-\left(\frac{\sqrt{2}}{\beta} \alpha\right)^2}$$

- **Beckmann**

- $m$  : root mean square
- Used by Cook-Torrance

$$D(\alpha) = \frac{1}{4m^2 \cos^4 \alpha} e^{-[\tan \alpha / m]^2}$$

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# Geometric Attenuation Factor

- **V-shaped grooves**
- Fully illuminated and visible

$$G = 1$$

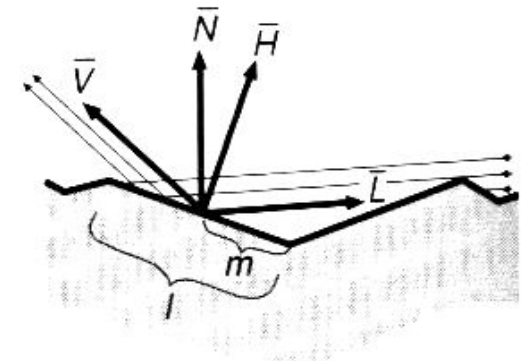
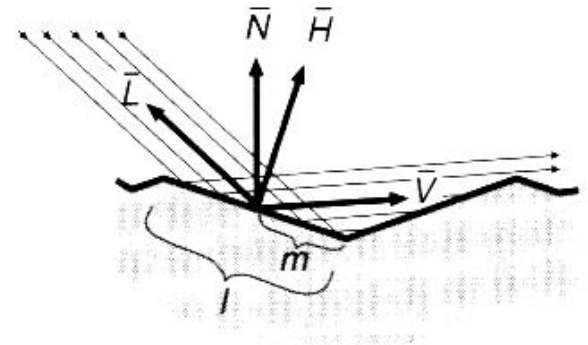
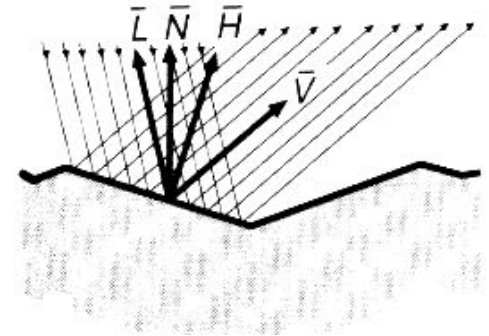
- Partial masking of reflected light

$$G = \frac{2(\underline{N} \cdot \underline{H})(\underline{N} \cdot \underline{V})}{(\underline{V} \cdot \underline{H})}$$

- Partial shadowing of incident light

$$G = \frac{2(\underline{N} \cdot \underline{H})(\underline{N} \cdot \underline{I})}{(\underline{V} \cdot \underline{H})}$$

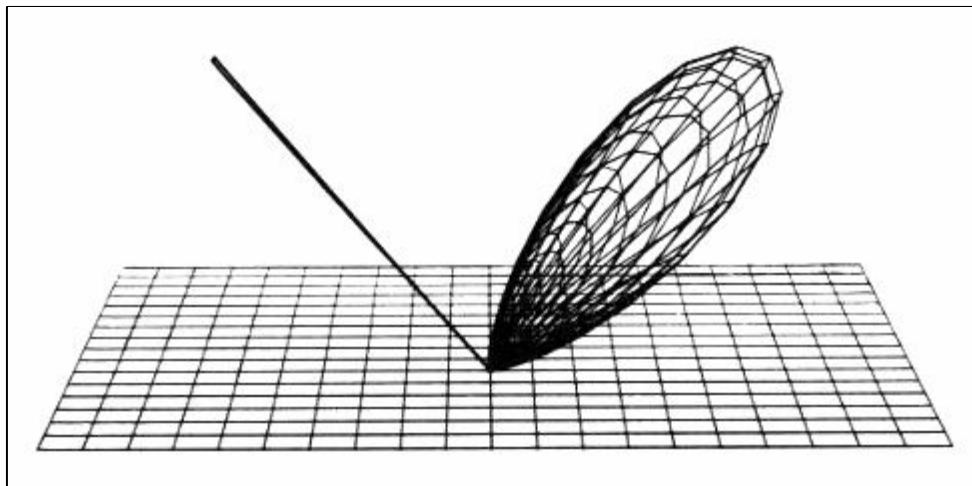
$$G = \min \left\{ 1, \frac{2(\underline{N} \cdot \underline{H})(\underline{N} \cdot \underline{V})}{(\underline{V} \cdot \underline{H})}, \frac{2(\underline{N} \cdot \underline{H})(\underline{N} \cdot \underline{I})}{(\underline{V} \cdot \underline{H})} \right\}$$



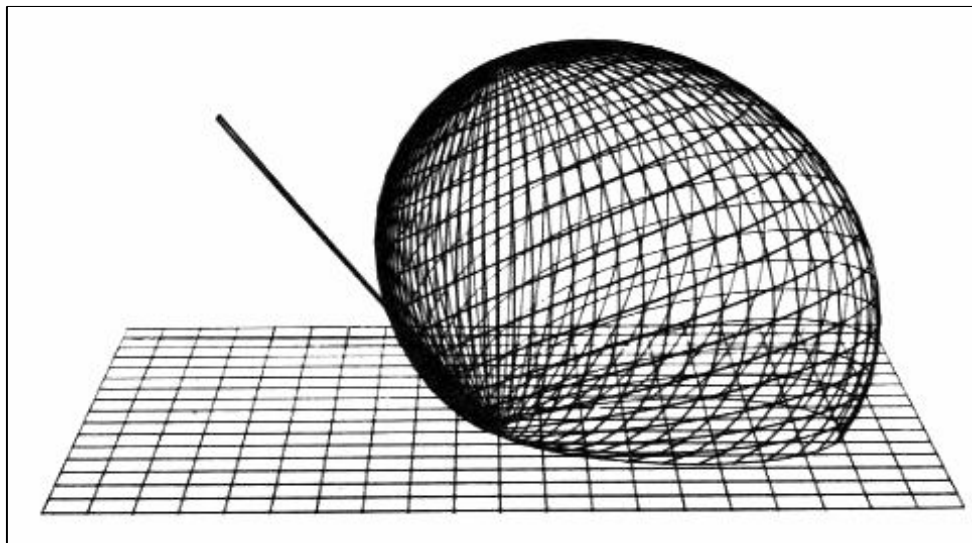
# Beckman Microfacet Distribution Function

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$m=0.2$

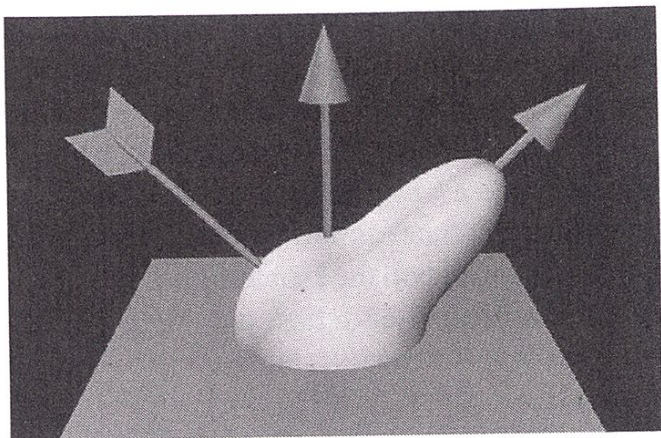


$m=0.6$

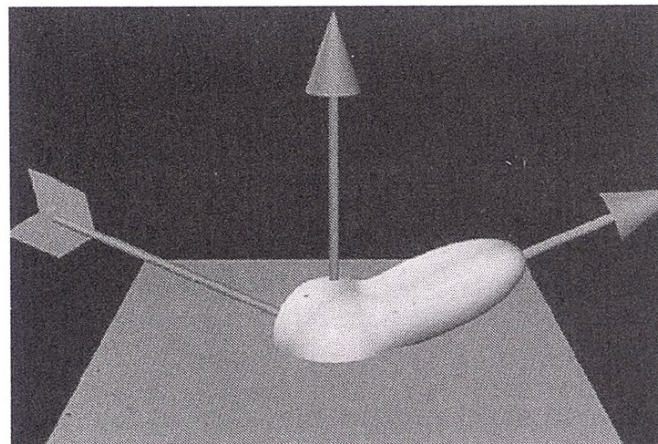


# Comparison Phong vs. Torrance

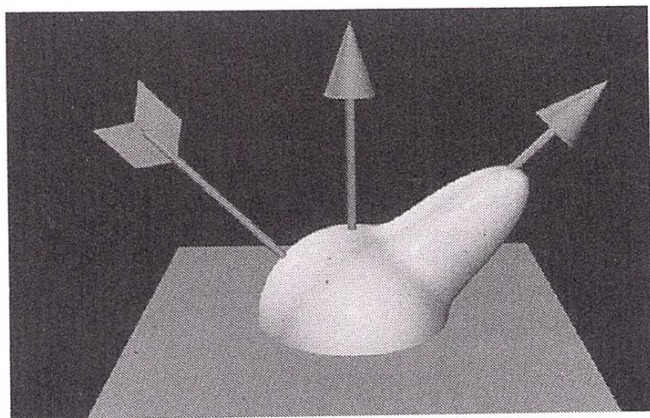
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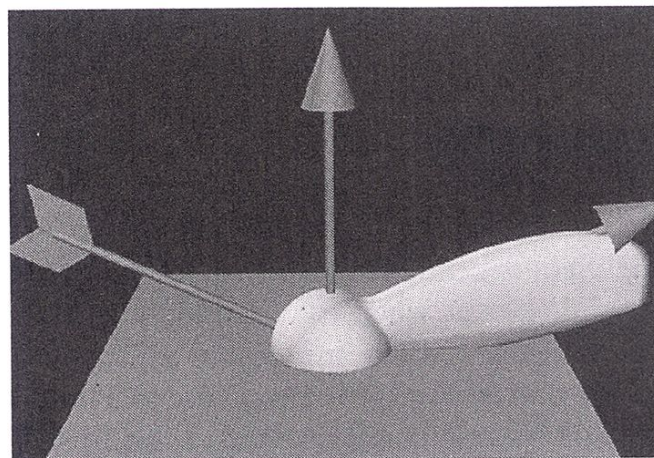
(a)



(b)



(c)



(d)

# Polygon-Shading Methods

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- Application of an illumination model to compute intensity for every pixel has been time consuming.
  - Intensity of adjacent pixels is usually very similar (the so called shading coherence), which allows for less frequent shading evaluations.
  - Each polygon can be rendered with a single intensity or intensity can be obtained at each point of the surface using an interpolation scheme:
    - **Flat shading**, single intensity is calculated for each polygon
    - **Gouraud shading** (per vertex shading), intensity calculated at vertices is interpolated across the surface
    - **Phong shading** (per pixel shading), normal vectors are calculated at vertices; then normal vectors are interpolated across the surface and an illumination model using these normal vectors is applied for every point of the surface
  - With modern hardware this is no big issue any more
    - Often even the normal is calculated per pixel
      - Bump or displacement maps
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# Problems in Interpolated Shading

- **Problems**

- Polygonal silhouette may not match the smooth shading
- Perspective distortion
  - Interpolation may be performed after perspective transformation in the 2-D screen coordinate system, rather than world coordinate system.
- Orientation dependence.
  - This problem does not concern triangles for which linear interpolation is rotation-invariant.
- Shading discontinuities at shared vertices (T-edges).
- Unrepresentative normal vectors.

