
2-AIN-108: Labs #5 DL Conceptualization

Exercise 1. Given Person , Female and hasChild define complex concepts:

- Male
- Parent
- Father
- Mother
- GrandParent
- GrandMother
- GrandFather
- MotherHavingOnlyDaughters

Exercise 2. Formalize following sentences as composite concepts:

- A man that is married to a doctor, and all of whose children are either doctors or professors.
- A man that likes only married women.
- A parent that has a child whose children are all married.

Exercise 3. Formalize following sentences as TBox axioms:

- Car engine is either diesel engine, petrol engine, electric engine, hybrid engine or steam engine.
- Vegetarians eat only vegetable.
- Vegan does not eat any animal product.
- Only humans can have human children.

Exercise 4. Prove following equivalences¹:

1. $\models C \sqcap \neg C \equiv \perp$
2. $\models C \sqcup \neg C \equiv \top$
3. $\models \neg \neg C \equiv C$
4. $\models \neg(C \sqcup D) \equiv \neg C \sqcap \neg D$
5. $\models \neg(C \sqcap D) \equiv \neg C \sqcup \neg D$

¹Hint: realize what does $\models C \equiv D$ mean, apply interpretation rules for concept constructors and prove resulting set identities.