

Updates of Hybrid Knowledge Bases

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Part I: What's the Problem?

Hybrid Knowledge Bases

Description Logics

- ✓ standard first-order semantics
- ✓ open world assumption
- ✓ expressivity vs. computational complexity
- ✓ implementations
- ✗ poor set of primitives regarding binary predicates (roles)
- ✗ no closed world reasoning
- ✗ hard to express integrity constraints

Logic Programs

- ✓ help resolve the above mentioned problems
- ✓ well-understood declarative semantics
- ✓ good computational properties

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- ✗ semantic issues (OWA vs. CWA)
- ✗ pragmatic problems (decidability)

A number of approaches proposed

- CARIN [Levy and Rousset, 1998]
- \mathcal{AL} -log [Donini et al., 1998]
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- ✓ theoretically neat
- ✓ tight integration between the two distinct formalisms
- ✓ generalise most previous approaches
- ✓ known how to achieve decidability and tractability

Example (Cargo Imports Knowledge Base)

$\text{Admissible}(I) \leftarrow \sim \text{SuspectedBadGuy}(I).$

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$\text{LowRisk} \equiv \text{Approved} \sqcap (\exists \text{From.EUCountry})$

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Evolution of Hybrid Knowledge Bases

Knowledge **evolves** with time.

Example (Cargo Import Knowledge Base Updates)

$c : (\neg \text{LowRiskCommodity})$

$\sim \text{ApprovedImporterOf}(i, C) \leftarrow \text{Tomato}(C).$

Overall Goal

Deal with updates of Hybrid Knowledge Bases.

What is out there?

- Belief Update
- Rule Update

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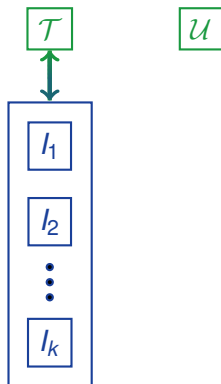
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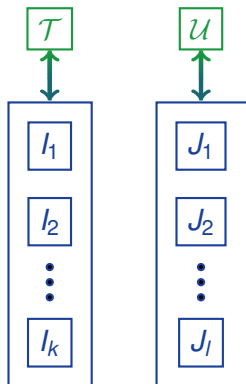
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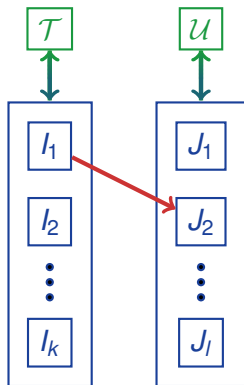
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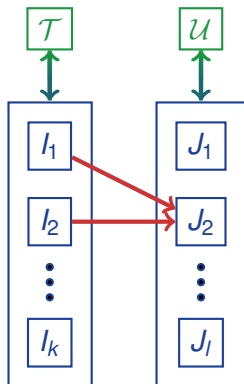
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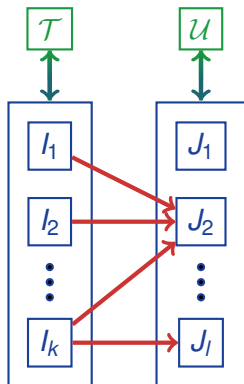
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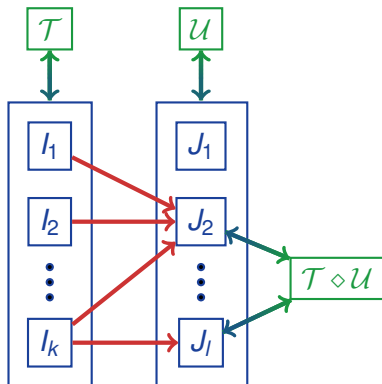
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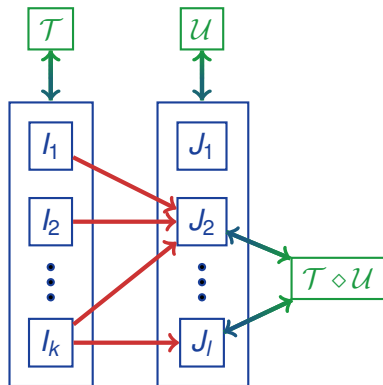
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- Winslett's operator \diamond^W – minimizes set difference

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- operator class \Leftrightarrow properties = representation theorem

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Theorem (Representation Theorem Template)

Let \mathcal{C} be a (constructively defined) class of operators, \mathcal{P} a set of properties and \diamond an update operator.

Then \diamond belongs to \mathcal{C} if and only if \diamond satisfies properties from \mathcal{P} .

Belief Update on DL Ontologies

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 - ✗ computational complexity
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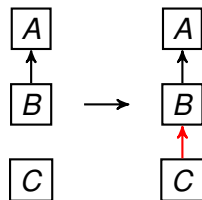
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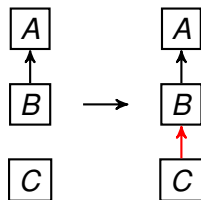
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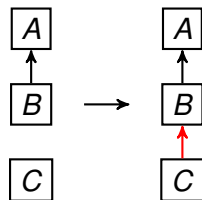


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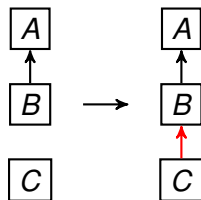
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Theorem (Unsuitability of Belief Update for TBoxes)

It is *impossible* for an update operator to satisfy (KM 3), (KM 4), (KM 8) and the two properties above.

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Belief Update is **very far from** a solution to ontology updates

Theorem (Unsuitability of Belief Update for TBoxes)

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- belief update approach is problematic
 - (KM 4): equivalent updates of equivalent programs lead to equivalent results
 - (KM 4) + stable or strong equivalence = catastrophe

$$\mathcal{P}_1 : \begin{array}{l} a. \\ b. \end{array} \quad \mathcal{P}_2 : \begin{array}{l} a \leftarrow b. \\ b. \end{array} \quad \mathcal{P} : \sim b.$$

• [Lindholm: Dynamic Logic Programming](#)

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• [Lecture 14: Dynamic Logic Programming](#)

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- based on rationality postulates
- syntax-insensitive
- inertia applied to atoms
- NP-hard in general
- polynomial for ABox updates in certain Description Logics

DLP

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Combining them is difficult!

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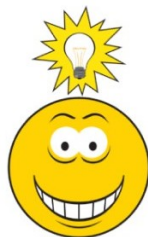
Logics

them

Part II: Addressing the Problem

1. Static Rules and Dynamic ABox

- rules: static queries, policies, business rules, strategies, preferences. . .
- TBox: static relations between roles and concepts
- a sequence of ABoxes: dynamically changing assertions about individuals in concepts and roles
- we proposed a solution for this scenario and investigated its basic properties



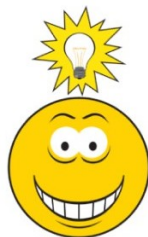
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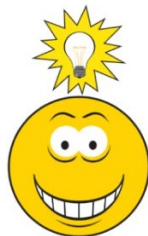
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1. Static Rules and Dynamic ABox (Technicalities)

- we defined semantics for a normal logic program \mathcal{P} updated by an ABox sequence $\mathcal{A} = (\mathcal{A}_1, \dots, \mathcal{A}_n)$ in the presence of a TBox \mathcal{T}
- M is a **stable model** of a normal logic program \mathcal{P} iff M is the least fixed point of $T_{\mathcal{P}^M}$ where \mathcal{P}^M is the Gelfond-Lifschitz reduct of \mathcal{P} w.r.t. M and

$$T_{\mathcal{P}}(M) = \{ H(r) \mid r \in \mathcal{P} \wedge M \models B(r) \}$$

Definition (Minimal Change Dynamic Stable Model)

M is a **minimal change dynamic stable model** of $\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}$ iff M is the least fixed point of $T_{\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}}$ where

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1. Static Rules and Dynamic ABox (Properties)

- ✓ Primacy of new information
- ✓ Syntax-independence w.r.t. to \mathcal{T} and \mathcal{A}
- ✓ Generalisation of stable model semantics
- ✓ Generalisation of Winslett's update semantics
- ✓ Immunity to empty updates

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Proposition

Let \mathcal{P} be a finite ground program, \mathcal{T} a TBox, \mathcal{A} an ABox and M a minimal change dynamic stable model of $\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}$. Then $M \models \mathcal{A}$.

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Proposition

Let \mathcal{P} be a finite ground program, $\mathcal{T}, \mathcal{T}'$ be TBoxes such that $\text{mod}(\mathcal{T}) = \text{mod}(\mathcal{T}')$, $\mathcal{A}, \mathcal{A}'$ be ABoxes such that $\text{mod}(\mathcal{A}) = \text{mod}(\mathcal{A}')$ and M be an MKNF interpretation. Then M is a minimal change dynamic stable model of $\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}$ if and only if M is a minimal change dynamic stable model of $\mathcal{P} \oplus^{\mathcal{T}'} \mathcal{A}'$.

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Let \mathcal{P} be a finite ground program. Then M is a stable model of \mathcal{P} if and only if M is a minimal change dynamic stable model of $\mathcal{P} \oplus^{\emptyset} \emptyset$.

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Proposition

Let \mathcal{P} be a finite ground program, \mathcal{T} be a TBox and $\mathcal{A} = (\mathcal{A}_1, \mathcal{A}_2, \dots, \mathcal{A}_n)$ a sequence of ABoxes (where $n \geq 1$). Let $\mathcal{A}' = (\mathcal{A}_1, \mathcal{A}_2, \dots, \mathcal{A}_{i-1}, \mathcal{A}_i, \emptyset, \mathcal{A}_{i+1}, \dots, \mathcal{A}_n)$ for some $i \in \{0, 1, 2, \dots, n\}$. Then an MKNF interpretation M is a minimal change dynamic stable model of $\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}$ if and only if M is a minimal change dynamic stable model of $\mathcal{P} \oplus^{\mathcal{T}} \mathcal{A}'$.

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2. Modular Update Semantics

- it is frequently possible to identify distinct **ontology layers** and **rule layers** in a hybrid knowledge base
- define a **modular update semantics** for these cases
- based on a **splitting theorem** for hybrid MKNF knowledge bases



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\mathcal{K}

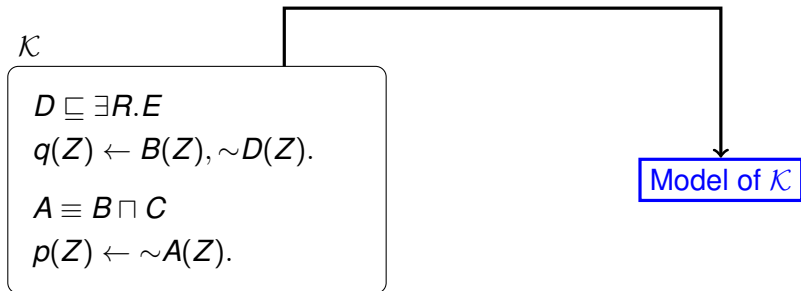
$$D \sqsubseteq \exists R.E$$

$$q(Z) \leftarrow B(Z), \sim D(Z).$$

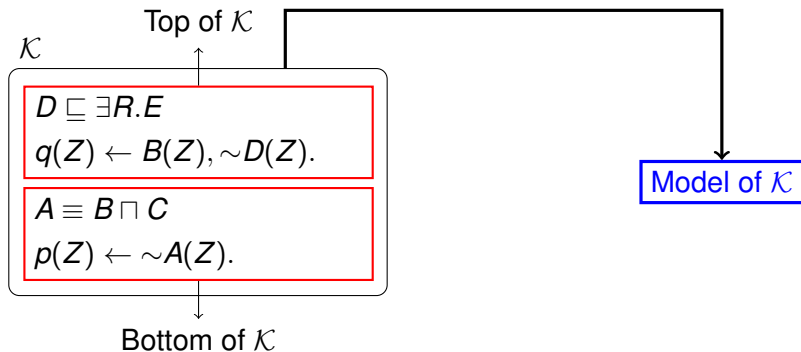
$$A \equiv B \sqcap C$$

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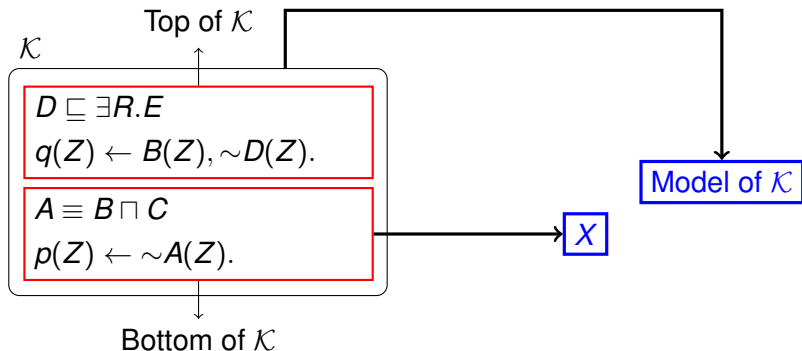
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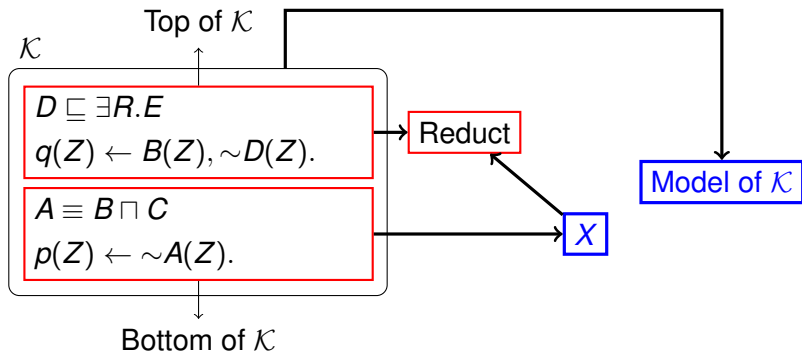
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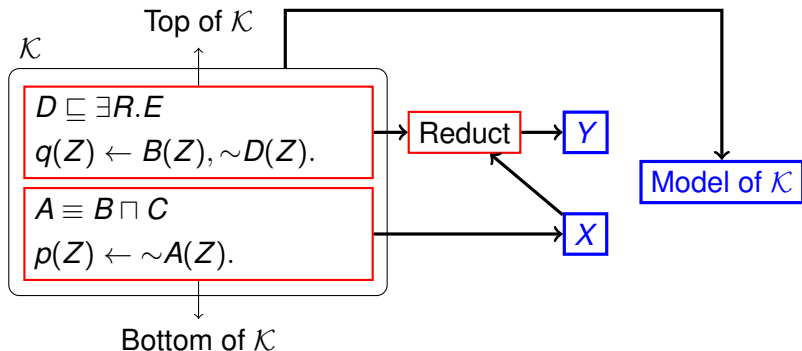
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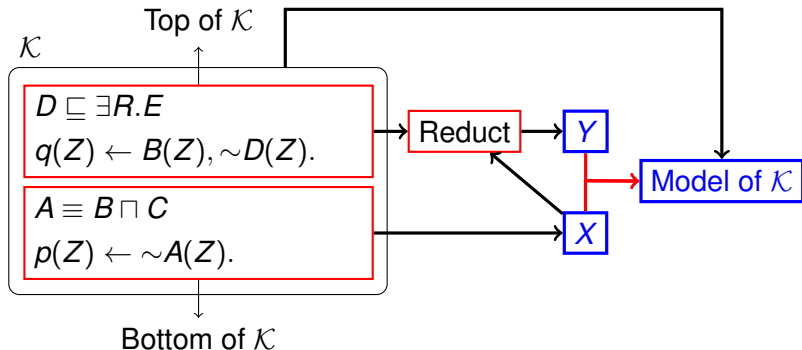
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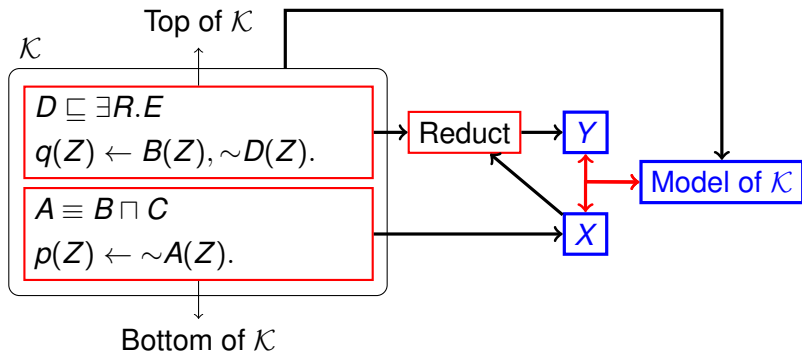
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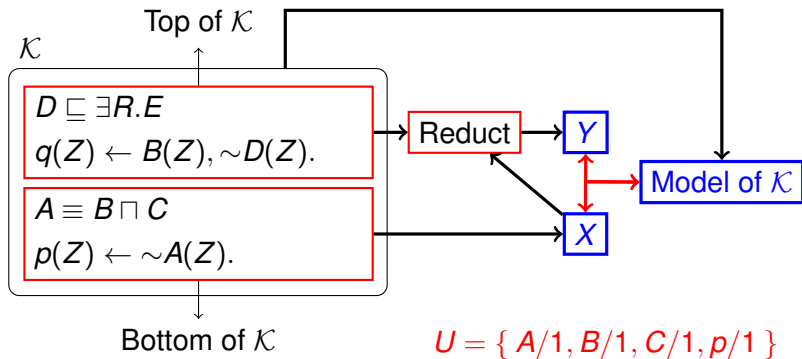
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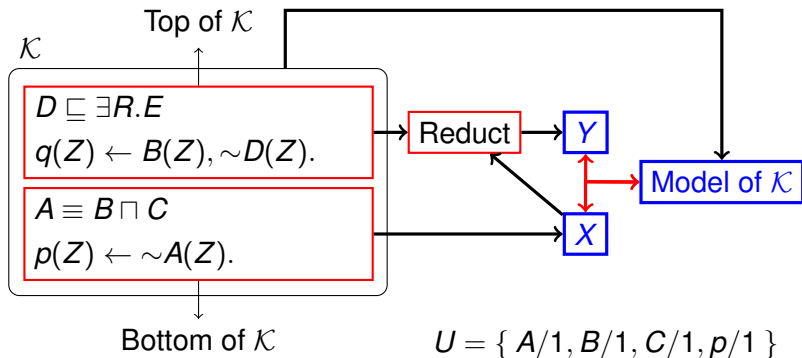
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Theorem (Splitting Theorem)

Let U be a splitting set for a hybrid knowledge base \mathcal{K} .
Then M is an MKNF model of \mathcal{K} if and only if $M = X \cap Y$
for some solution $\langle X, Y \rangle$ to \mathcal{K} w.r.t. U .

2. Modular Update (Splitting Sequence Theorem)

Definition (Splitting Sequence)

A **splitting sequence** for a hybrid knowledge base \mathcal{K} is a monotone, continuous sequence $U = \langle U_\alpha \rangle_{\alpha < \mu}$ of splitting sets for \mathcal{K} such that $\bigcup_{\alpha < \mu} U_\alpha = \mathbf{P}$.

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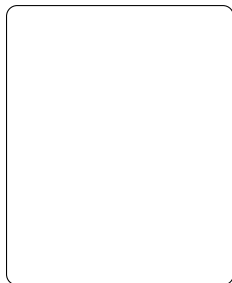
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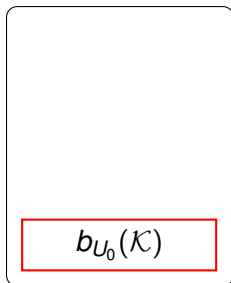


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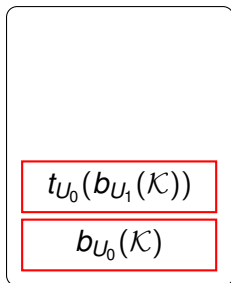


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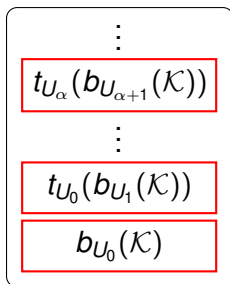


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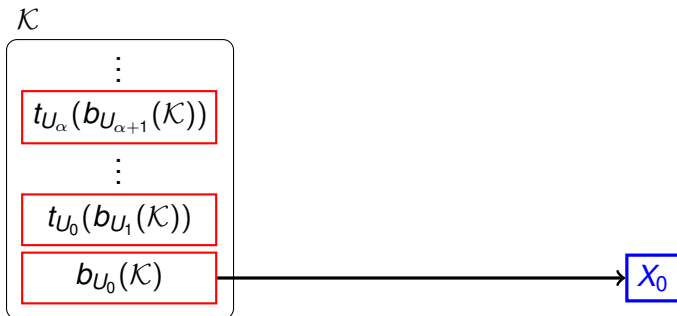
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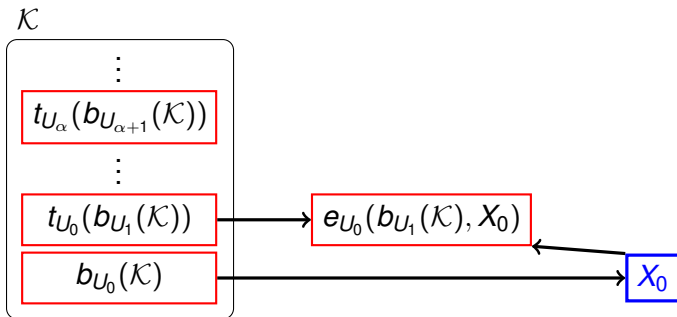
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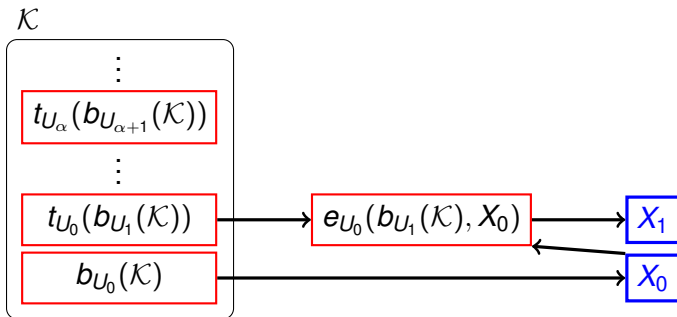
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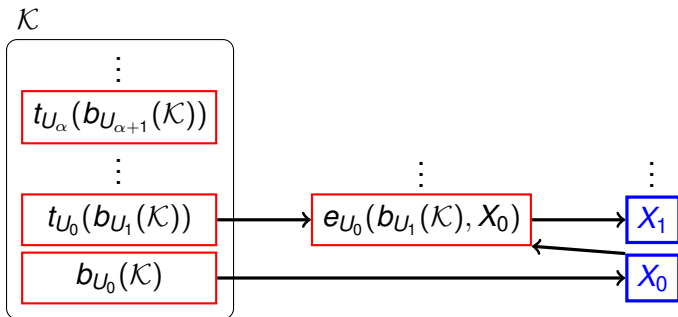
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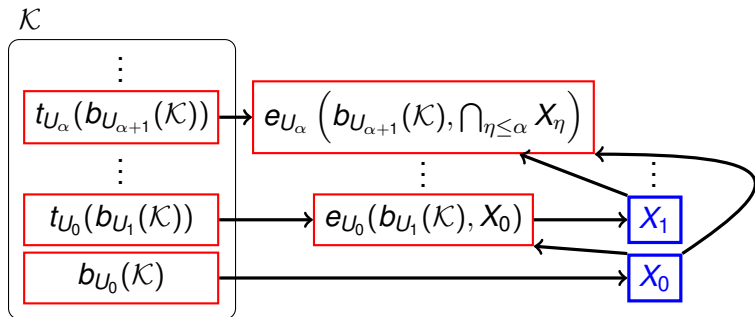
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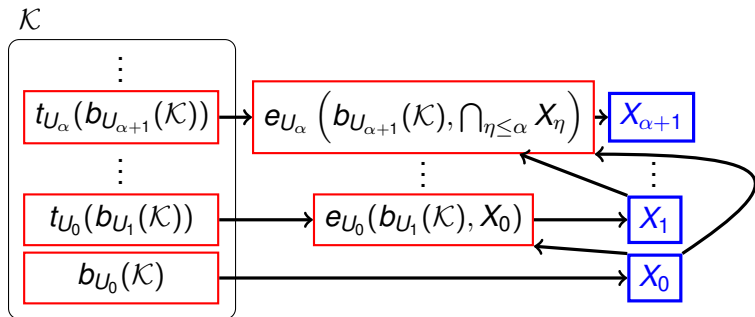
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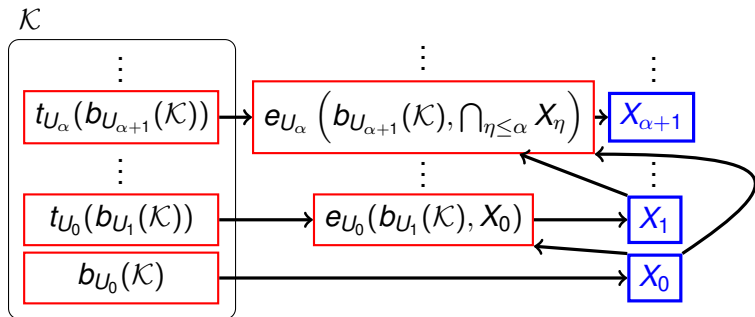
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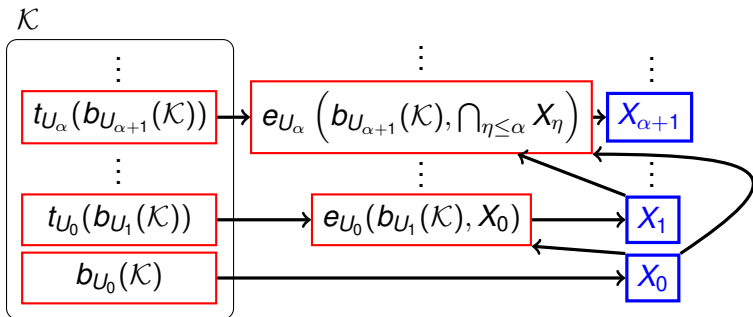
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The sequence $\langle X_\alpha \rangle_{\alpha < \mu}$ is a **solution to \mathcal{K} w.r.t. U** .

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Theorem (Splitting Sequence Theorem)

Let $U = \langle U_\alpha \rangle_{\alpha < \mu}$ be a splitting sequence for a hybrid knowledge base \mathcal{K} . Then M is an MKNF model of \mathcal{K} if and only if $M = \bigcap_{\alpha < \mu} X_\alpha$ for some solution $\langle X_\alpha \rangle_{\alpha < \mu}$ to \mathcal{K} w.r.t. U .

2. Modular Update Semantics (Operator)

Question

Given

- an update semantics for $\langle \mathcal{O}_i \rangle_{i < n}$ and
- an update semantics for $\langle \mathcal{P}_i \rangle_{i < n}$,

to what type of $\mathcal{K} = \langle \mathcal{K}_i \rangle_{i < n}$ can we **easily assign** an update semantics?

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Definition

Let $U = \langle U_\alpha \rangle_{\alpha < \mu}$ be an update-enabling splitting sequence for a dynamic hybrid knowledge base \mathcal{K} . We say that an MKNF interpretation M is a **dynamic MKNF model of \mathcal{K} w.r.t. U** if $M = \bigcap_{\alpha < \mu} X_\alpha$ for some solution $\langle X_\alpha \rangle_{\alpha < \mu}$ to \mathcal{K} w.r.t. U .

2. Modular Update Semantics (Properties)

Using particular update operators:

- 1 Winslett's minimal change update operator [Winslett, 1990]
- 2 Refined dynamic stable models [Alferes et al., 2005]

3 Independence of Solving Sequence

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Theorem (Independence of Splitting Sequence)

Let U, V be update-enabling splitting sequences for a dynamic hybrid knowledge base \mathcal{K} . Then M is a dynamic MKNF model of \mathcal{K} w.r.t. U if and only if M is a dynamic MKNF model of \mathcal{K} w.r.t. V .

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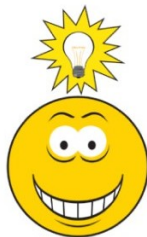
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- (KM 4) + stable or strong equivalence
= catastrophe

\mathcal{P}_1 : a. \mathcal{P}_2 : a \leftarrow b. \mathcal{P} : \sim b.
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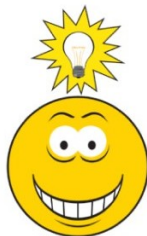


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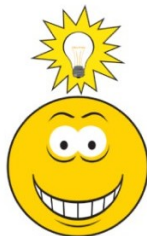


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- 1 by restricting the dynamic part of the knowledge base
- 2 by restricting interaction between DL axioms and rules
- 3 by aiming to create semantic counterparts of the rule update semantics

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- DL ontology update
 - principles in line with intuitions
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Thank you!

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- José Júlio Alferes, Federico Banti, Antonio Brogi, and João Alexandre Leite. The refined extension principle for semantics of dynamic logic programming. [Studia Logica](#), 79(1):7–32, 2005. URL <http://centria.di.fct.unl.pt/~jja/page3/assets/sl05.pdf>.
- Francesco M. Donini, Maurizio Lenzerini, Daniele Nardi, and Andrea Schaerf. AL-log: Integrating datalog and description logics. [Journal of Intelligent Information Systems](#), 10(3): 227–252, 1998.
- Thomas Eiter, Thomas Lukasiewicz, Roman Schindlauer, and Hans Tompits. Combining answer set programming with description logics for the semantic web. In Didier Dubois, Christopher A. Welty, and Mary-Anne Williams, editors, [Proceedings of the 9th International Conference on Principles of Knowledge Representation and Reasoning](#)

(KR2004), pages 141–151, Whistler, Canada, June 2-5 2004. AAAI Press. URL http://www.kr.tuwien.ac.at/staff/eiter/et-archive/kr04-dl_asp.pdf.

Thomas Eiter, Giovambattista Ianni, Roman Schindlauer, and Hans Tompits. A uniform integration of higher-order reasoning and external evaluations in answer-set programming. In Leslie Pack Kaelbling and Alessandro Saffiotti, editors, [Proceedings of the 19th International Joint Conference on Artificial Intelligence \(IJCAI-05\)](#), pages 90–96, Edinburgh, Scotland, UK, July 30-August 5 2005. Professional Book Center. ISBN 0938075934.

Benjamin N. Grosf, Ian Horrocks, Raphael Volz, and Stefan Decker. Description logic programs: Combining logic programs with description logic. In [Proceedings of the 12th International World Wide Web Conference \(WWW 2003\)](#), pages 48–57, Budapest, Hungary, May 20-24 2003. ACM. ISBN 1-58113-680-3. URL

[http://www.cs.man.ac.uk/~horrocks/
Publications/download/2003/p117-grosf.pdf](http://www.cs.man.ac.uk/~horrocks/Publications/download/2003/p117-grosf.pdf).

Ian Horrocks, Peter F. Patel-Schneider, Harold Boley, Said Tabet, Benjamin Grosf, and Mike Dean. SWRL: A semantic web rule language. W3C Member Submission 21 May 2004, <http://www.w3.org/Submission/SWRL/>, 2004. URL

Latest version available at <http://www.w3.org/Submission/SWRL/>.

Markus Krötzsch, Sebastian Rudolph, and Pascal Hitzler. Description logic rules. In Malik Ghallab, Constantine D. Spyropoulos, Nikos Fakotakis, and Nikos Avouris, editors, [Proceedings of the 18th European Conference on Artificial Intelligence \(ECAI2008\)](#), pages 80–84, Patras, Greece, July 2008. IOS Press. URL

<http://www.aifb.uni-karlsruhe.de/WBS/phi/resources/publications/dlrules-ecai08.pdf>.

Alon Y. Levy and Marie-Christine Rousset. Combining horn rules and description logics in CARIN. [Artificial Intelligence](#), 104(1-2):165–209, 1998. URL

<http://www.cs.washington.edu/homes/alon/files/aij-carin.pdf>.

- Vladimir Lifschitz. Nonmonotonic databases and epistemic queries. In [Proceedings of the 12th International Joint Conference on Artificial Intelligence \(IJCAI'91\)](#), pages 381–386, 1991. URL <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.105.5424&rep=rep1&type=pdf>.
- Boris Motik and Riccardo Rosati. Reconciling description logics and rules. [Journal of the ACM](#), 57(5):93–154, 2010.
- Riccardo Rosati. Towards expressive kr systems integrating datalog and description logics: preliminary report. In Patrick Lambrix, Alexander Borgida, Maurizio Lenzerini, Ralf Möller, and Peter F. Patel-Schneider, editors, [Proceedings of the 1999 International Workshop on Description Logics \(DL'99\)](#), volume 22 of [CEUR Workshop Proceedings](#), Linköping, Sweden, July 30 - August 1 1999. CEUR-WS.org.

Riccardo Rosati. DL+log: Tight integration of description logics and disjunctive datalog. In Patrick Doherty, John Mylopoulos, and Christopher A. Welty, editors, [Proceedings of the 10th International Conference on Principles of Knowledge Representation and Reasoning \(KR2006\)](#), pages 68–78, Lake District of the United Kingdom, June 2-5 2006. AAAI Press. ISBN 978-1-57735-271-6. URL

<http://www.dis.uniroma1.it/~rosati/publications/Rosati-KR-06.pdf>.

Martin Slota and João Leite. Towards Closed World Reasoning in Dynamic Open Worlds. [Theory and Practice of Logic Programming, 26th Int'l. Conference on Logic Programming \(ICLP'10\) Special Issue](#), 10(4-6):547–564, July 2010. URL

<http://slotik.info/sites/slotik.info/files/Slota2010a.pdf>.

Marianne Winslett. [Updating Logical Databases](#). Cambridge University Press, New York, NY, USA, 1990. ISBN 0-521-37371-9.