
Computer Graphics

- Scan Conversion -

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Overview

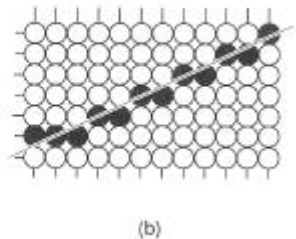
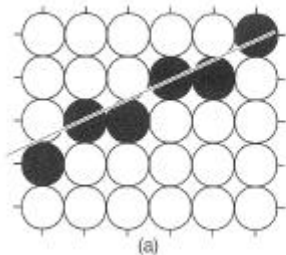
- **So far:**
 - Clipping
 - Rasterization

- **Today:**
 - Antialiased lines
 - Scan conversion
 - Edge coherence
 - Span coherence
 - Interpolation

- **Next time:**
 - Cg

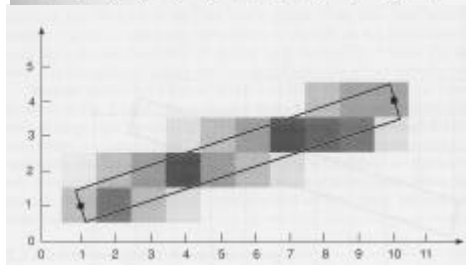
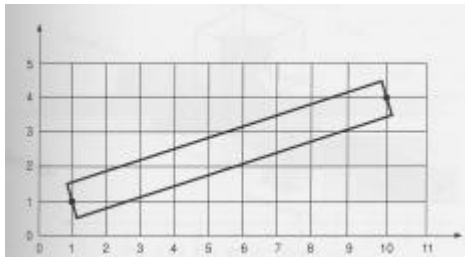
Antialiased Line Drawing

- **Aliasing effects**
 - Moire patterns
 - Staircase, jaggies
- **Trivial solution: Increasing resolution**
 - 4x memory, bandwidth, rendering time
 - Reduces aliasing, doesn't eliminate



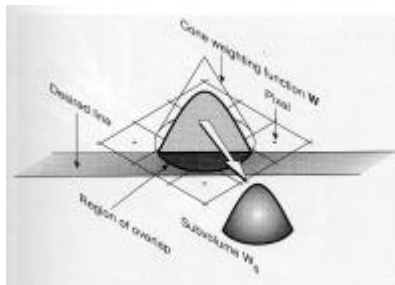
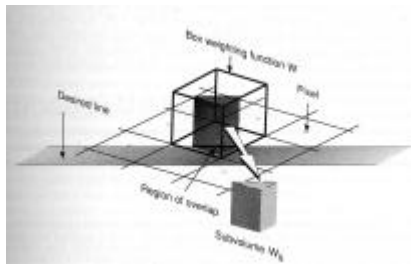
Unweighted Area Sampling

- **Line has finite area**
 - Draw rectangle
- **Intensity distribution**
 - According to percentage covered
 - Only intersected pixels affected
- **Unweighted sampling**
 - Equal areas contribute equally
 - Entire pixel area of equal weight
 - distance pixel center - line no criterion



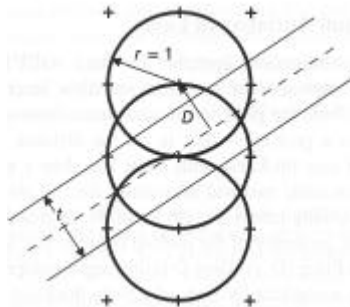
Weighted Area Sampling

- **Equal areas contribute unequally**
 - Area close to pixel center has greater influence
- **Weighting function**
 - Centered on each pixel
 - Integral = 1
 - Larger than pixel diameter
 - Weighted intersection area with line rectangle: intensity
- **Unweighted Sampling**
 - Box filter
- **Weighted Sampling**
 - Cone filter



Cone-filtered Line Drawing

- **Gupta-Sproull algorithm**
- **Need to know smallest distance from line to pixel center D**
 - Weighted intersected line area:
table lookup $W(D,t)$
 - t : line thickness
- **Bresenham**
 - Decision variable d to find mid-line pixel
 - Intensity for mid-pixel and both vertically neighboring pixels ?
 - Distance pixels' center – line D



Antialiased Bresenham Lines

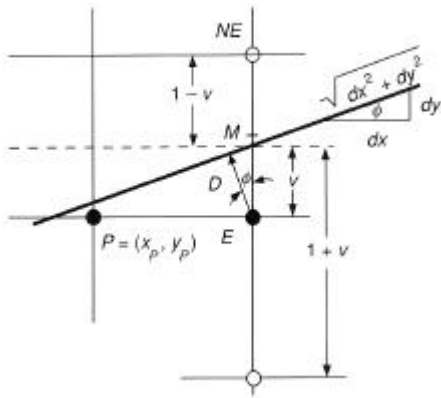
- Distance to line center

$$D = v \cos f = \frac{v dx}{\sqrt{dx^2 + dy^2}}$$

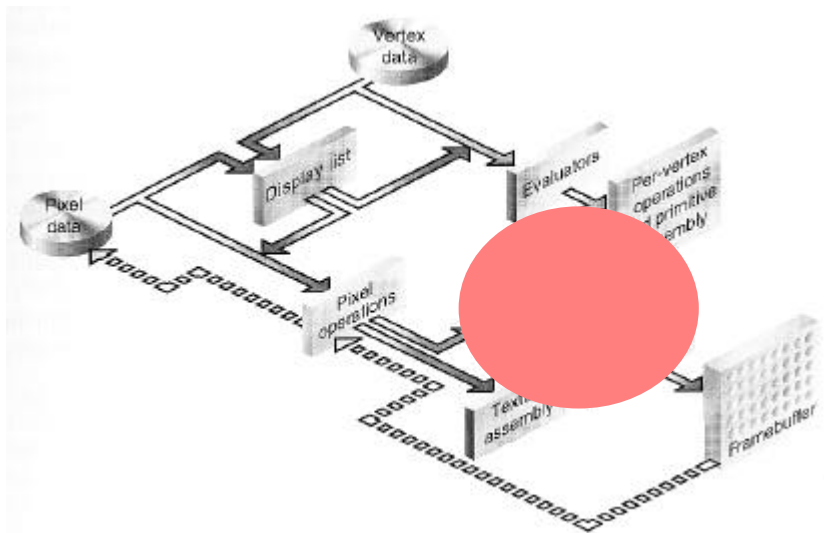
- In incremental form

$$D_{closest} = \frac{d \pm 1}{2\sqrt{\Delta x^2 + \Delta y^2}}$$

$$D_{\pm 1} = \frac{2 \pm (d \pm 1)}{2\sqrt{\Delta x^2 + \Delta y^2}}$$



We are here ...



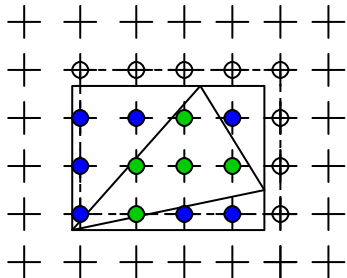
Scene-to-Screen Conversion

- **Scene composed of primitives**
- **Rendering:**
 - Determine 2D projection coordinates of each primitive
 - Per-vertex transformations
 - Find screen pixels covered by primitive
 - Clipping
 - rasterization
 - Handle occlusions between primitives
 - Hidden surface removal
 - Calculate pixel colors from visible primitives
 - shading

Triangle Filling

- **Brute-Force algorithm**

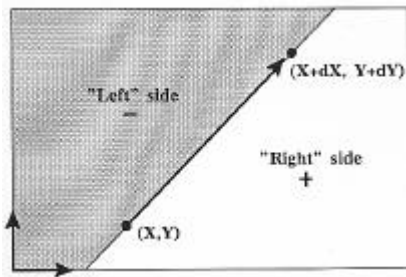
```
Raster3_box(vertex v[3])
{
    int x, y;
    bbox b;
    bound3(v, &b);
    for (y= b.ymin; y < b.ymax; y++)
        for (x= b.xmin; x < b.xmax; x++)
            if (inside(v, x, y))
                fragment(x,y);
}
```



Inside-Outside Test for Triangles

- **Approach**

- Implicit edge functions to describe the triangle
 $F_i(x,y) = ax+by+c$
- Point inside triangle, if every $F_i(x,y) \leq 0$
- Incremental evaluation of the linear function F by adding a or b

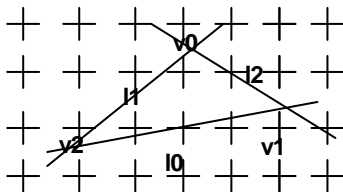


Incremental Rasterization Process

```
Raster3_incr(vertex v[3])
{
    edge l0, l1, l2;
    value d0, d1, d2;
    bbox b;
    bound3(v, &b);
    mkedge(v[0],v[1],&l2);
    mkedge(v[1],v[2],&l0);
    mkedge(v[2],v[0],&l1);

    d0 = l0.a * b.xmin + l0.b * b.ymin + l0.c;
    d1 = l1.a * b.xmin + l1.b * b.ymin + l1.c;
    d2 = l2.a * b.xmin + l2.b * b.ymin + l2.c;

    for( y=b.ymin; y<b.ymax, y++ ) {
        for( x=b.xmin; x<b.xmax, x++ ) {
            if( d0<=0 && d1<=0 && d2<=0 ) fragment(x,y);
            d0 += l0.a; d1 += l1.a; d2 += l2.a;
        }
        d0 += l0.a * (b.xmin - b.xmax) + l0.b; . . . }
}
```

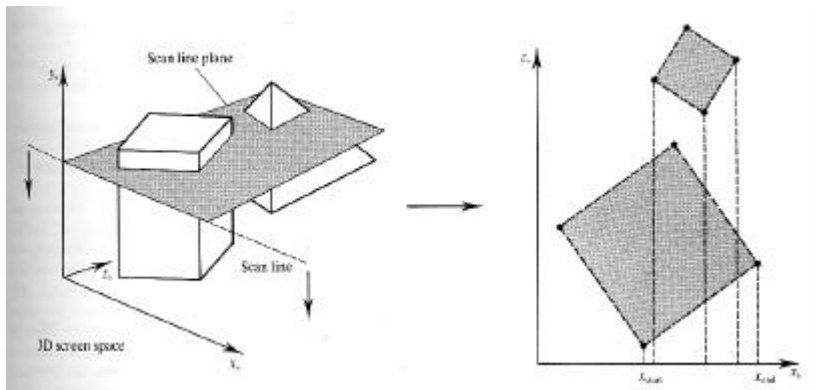


Coherence

- ***Adjacent pixels generally exhibit the same properties***
- If a given pixel is ***inside*** a polygon, then ***immediately adjacent*** pixels are also likely to be ***inside*** the polygon. The converse is also true.
- We say that the ***visibility*** of adjacent pixels differs only if an edge (or boundary) of the polygon passes between them - a relatively un-common event.

⇒ **Exploit pixel coherence
for efficient, fast polygon rendering**

Rasterization



- **3D screen space**
- **Scan line: horizontal line of screen**
- **Span: extension of polygonal edge on scan line**
 - From x_{start} to x_{end}

Pixel-Level Processes

- **Rasterization, hidden surface removal, shading**
 - Carried out in inner loop of renderer
 - Regard one polygon at a time
 - Regard one scan line at a time
 - Span: intersection of scan line with polygon
 - Conversion into run of consecutive pixels: exploits coherence
- **Two-dimensional linear interpolation processes**

For each scan line, find span

 - Limits / x-coordinates: **rasterization**
 - Interpolated from 2D edge vertex positions in screen space

For each span's limits, find

 - Scene depth: **hidden surface removal**
 - Interpolated from edge vertices' z-coordinate in screen space
 - Color/normal: **shading**
 - Interpolated from edge vertices' color/normal
 - Interpolate depth/color between span limits

Pixel-Level Processes

- **Innermost rendering loop**

```
for each polygon
{
    perform geometric transformations into screen space
    for each scan line within the polygon
    {
        find span by interpolation of edge vertex
        coordinates
        find span limits' depth & color/normal
        rasterize span
        for each pixel within the span
        {
            interpolate depth & color/normal from span
            limits
            perform hidden surface removal
            shade pixel
        }
    }
}
```

Rasterization

- **Definition**

- Given a primitive, specify which pixels on a raster display are covered by this primitive
- Extension: specify fraction of partially covered pixels
 - Antialiasing

- **Questions**

- Where exactly does a span start/end ?
- Where within the pixel should the sample point be ?
- Round screen coordinates to integer ?
Store with fractional precision ?

- **Problems**

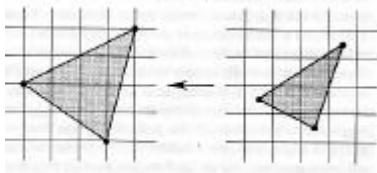
- Holes between polygons
- Overlapping polygons (problems with transparency)
- Discontinuities in textured surfaces
- Inaccuracies during anti-aliasing

Errors in Rasterization

Screen coordinates

- **Integer rasterization**

- Distorts shape
 - Correct supersampling not possible
 - Animation: “wobble”
 - Nearly vertical edge: step discontinuity
 - Shift in texture mapping
- ⇒ High precision necessary



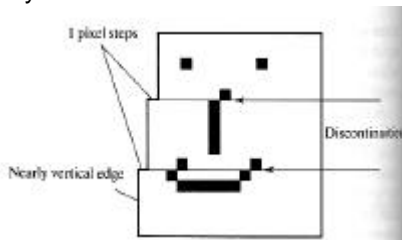
Sample point position

- **Pixel center**

- Unnecessary fractional-pel offset

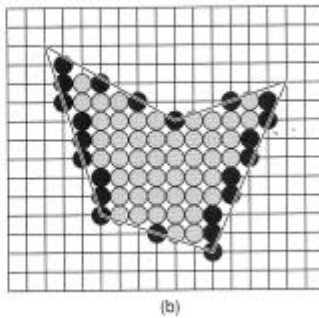
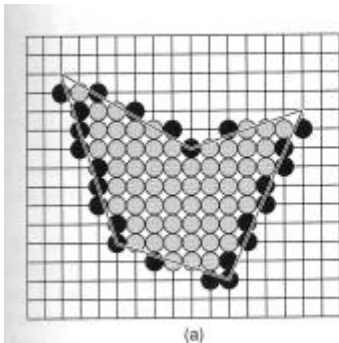
- **Pixel corner**

- Maximal $\frac{1}{2}$ -pixel displacement
- Doesn't matter as long as consistent



Polygon Edges

- **Bresenham: Closest pixels along edge lines**
 - Inside or outside polygon
 - Overdrawing from neighboring polygons, flickering
- **Combine with knowledge about per-scanline span**
 - Inside-outside: Odd-parity rule



Span Boundary Rounding



- **Real numbers**
 - Round x_{start} up
 - Round x_{end} down
 - If fractional part of x_{end} is 0, subtract 1
- **Integer arithmetic (4-bit example)**
 - Round x_{start} up to next multiple of 16
 - Round x_{end} down to next multiple of 16
 - If x_{end} is multiple of 16, subtract 16 from it
- **No holes between spans**
- **No overlap of span**
- **Generated pixels are always within span bounds**

Span Interpolation

- **Find x_{start} and x_{end} of span**
 - Linear interpolation between polygon edge endpoints
 - Floating point accuracy
 - Modified Bresenham algorithm
 - Integer arithmetic
- **Determine depth for each pixel**
 - Find depth at span boundaries
 - Linear interpolation between polygon edge endpoints
(z-coordinates of vertex positions in 3D screen space)
 - Linear interpolation between span boundaries
- **Determine color for each pixel**
 - Gouraud: Find color at span boundaries
 - Phong: Find normal direction at span boundaries
 - Linear interpolation between polygon edge endpoints
 - Linear interpolation between span boundaries

Efficient Scan Conversion

- **In which order to draw polygons/scanlines ?**
 - One polygon after the other
 - Frequent scanline jumps
 - One scanline after the other
 - considers pixels incrementally
 - Exploits pixel coherence
 - Acceleration data structures
 - E.g., triangle strips
- **Brute force: intersect all the edges with each scanline**
 - Find y_{min} and y_{max} of each edge
 - Intersect edge only when it crosses the scanline
 - Calculate the intersection of the edge with the first scan line it intersects
 - calculate dx/dy
 - for each additional scanline, calculate the new intersection as $x = x + dx/dy$

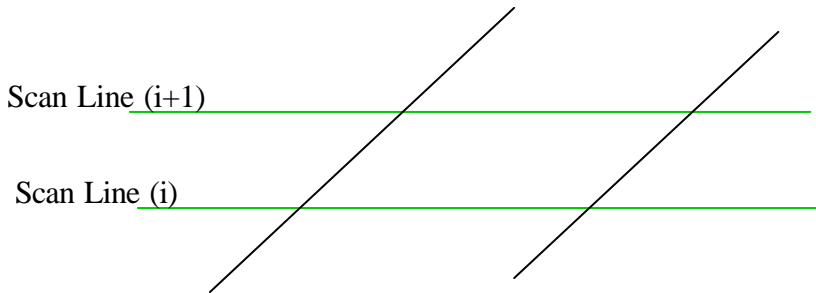
Edge Coherence Property

"Many of the edges intersected by scan line (i) will also be intersected by scan line (i + 1)."

Using the ***edge coherence*** property we can save time in computing the intersection of an edge with scan line **(i+1)** if we know:

- **the edge's intersection with scan line (i)**
- **the slope of the line segment m**

Moving from Scan-Line to Scan-Line



$$X_{(i+1)} = X_{(i)} + (1/m)$$

where: $m = dy / dx$

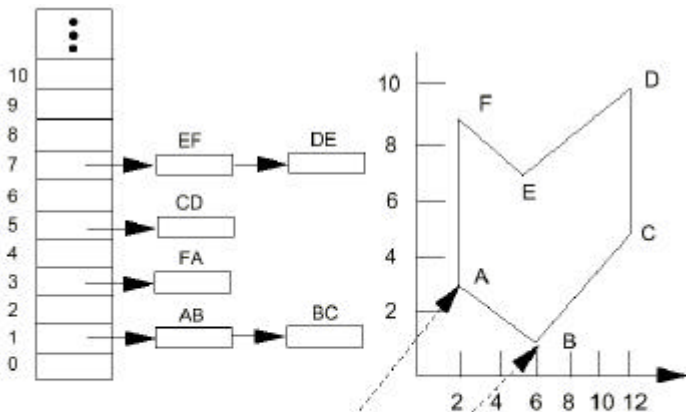
$$dy = 1 \implies dx = 1/m$$

Edge Table

- The Edge Table consists of a series of entries
- Each entry is a linked list

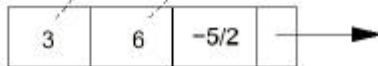
- All edges are sorted by their *ymin* coordinates
- keep a separate bucket for each scanline
- within each bucket, edges are sorted by increasing *x* of the *ymin* endpoint
- A scan line will have a non-empty linked list entry **ONLY** if it corresponds to the lower *y*-coordinate of a line segment

Edge Table



- Edge structure: ymax, xmin, dx/dy, next

AB:



Entry in the Linked List

- **An *entry* in the linked list contains (if an entry is needed):**
 - The **larger *y-coordinate*** of the ***edge*** (i.e., the ***maximum scan line***)
 - The ***x-coordinate*** of the ***lower (bottom)*** end point (X_{\min}) (i.e., the ***X*** value for Y_{\min})
 - The x increment used in stepping from one scan line to the next i.e. $1/m$
 - If necessary, a pointer to another entry in the linked list of this scan line
- **Incremental algorithm**
 - Utilization of coherence
 - along the edges
 - on scanlines
 - „sweep-line-algorithm“

Use of Active Edge List

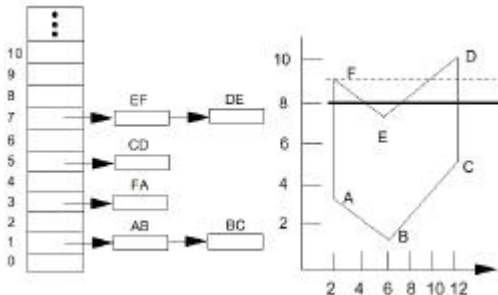
- Having created an **edge table**, we can scan (line by line) using only those edges relevant for that scan line.
- These are held in an **active edge list** which is created and maintained from the **edge table**.
- Moving from scan line to scan line, we calculate new x intersections using the equation:

$$x_{(i+1)} = x_{(i)} + 1/m$$

- Any new edges intersected by this next scan line are introduced (from the **edge table**) into the **active edge list** and edges not intersected by this next scan line are removed.
- This may involve sorting.

Active Edge List

- A list of edges active for current scanline, sorted in increasing x
- *Active edge list at*
 - $Y=8$



FA

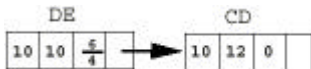
EF

DE

CD



- $Y=9$



Polygon Scan-Conversion Algorithm

Construct the Edge Table (ET);

Active Edge Table (AET) = null;

for y = Ymin to Ymax

 Merge-sort ET[y] into AET by x value

 Fill between pairs of x in AET

 for each edge in AET

 if edge.y_{max} = y

 remove edge from AET

 else

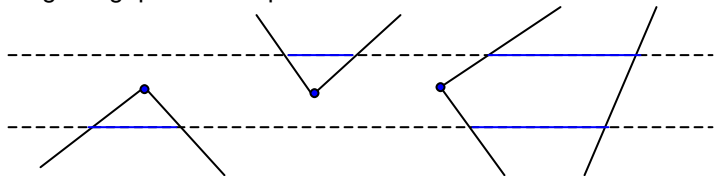
 edge.x = edge.x + dx/dy

 sort AET by x value

end scan_fill

Scanline Algorithm

- **For each scan line**
 - Update the Active -Edge-Table
 - Linked-list of entries
 - Link to edge-entries,
 - x, horizontal increment of depth, color, etc
 - Remove edges if their ymax is reached
 - Insert new edges (from Edge-Table)
 - Sorting
 - Incremental update of x
 - Sorting by X-coordinate of the intersection point with scanline
 - Filling the gap between pairs of entries



Polygon Scan-Conversion

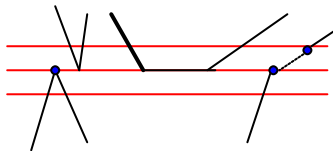
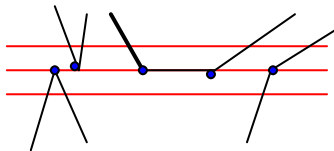
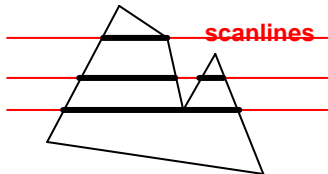
- **Special cases**

- Edge along a scanline

- $(x+e, y+e)$, shadow test:
 - draw the bottom edge
 - skip the top edge

- Vertex on a scanline

- If edges sharing the vertex are located on the **same side** of the scanline – properly handled
- If edges sharing the vertex are located on **opposite sides** of the scanline – one edge (top) is shortened: y_{\min}/y_{\max} rule



Wrap-Up

- **Per-pixel processes**
 - ⇒ Exploit pixel coherence
 - Rasterization
 - Shading
- **Scanline conversion**
 - Spans
 - Linear interpolation
 - Floating point accuracy
 - Correct rounding
- **Edge table**
- **Active edge list**