

$\text{Degree} \equiv \text{BachelorDegree} \sqcup \text{MasterDegree} \sqcup \text{DoctoralDegree}$   
 $\text{BachelorDegree} \sqsubseteq \neg \text{MasterDegree}$   
 $\text{BachelorDegree} \sqsubseteq \neg \text{DoctoralDegree}$   
 $\text{MasterDegree} \sqsubseteq \neg \text{DoctoralDegree}$   
 $\text{Bachelor} \equiv \exists \text{hasDegree}.\text{BachelorDegree}$   
 $\text{Master} \equiv \exists \text{hasDegree}.\text{MasterDegree}$   
 $\text{Doctor} \equiv \exists \text{hasDegree}.\text{DoctoralDegree}$   
 $\text{Bachelor} \sqsubseteq \text{Person}$   
 $\text{Master} \sqsubseteq \text{Bachelor}$   
 $\text{Doctor} \sqsubseteq \text{Master}$   
 $\text{Teacher} \equiv \exists \text{teaches}.\text{Course}$   
 $\text{Teacher} \sqsubseteq \text{Doctor}$   
 $\text{Assistant} \equiv \exists \text{assists}.\text{Course}$   
 $\text{Assistant} \sqsubseteq \text{Master}$   
 $\text{Student} \equiv \exists \text{attends}.\text{Course}$   
 $\text{Student} \sqsubseteq \text{Person}$   
 $\text{Student} \sqsubseteq \text{BachelorStudent} \sqcup \text{MasterStudent} \sqcup \text{DoctoralStudent}$   
 $\text{BachelorStudent} \sqsubseteq \text{Student} \sqcap \neg \text{Bachelor}$   
 $\text{MasterStudent} \sqsubseteq \text{Student} \sqcap \text{Bachelor} \sqcap \neg \text{Master}$   
 $\text{DoctoralStudent} \sqsubseteq \text{Student} \sqcap \text{Master} \sqcap \neg \text{Doctor}$   
 $\text{Person} \sqsubseteq \neg \text{Course}$   
 $\text{Degree} \sqsubseteq \neg \text{Person}$   
 $\text{Degree} \sqsubseteq \neg \text{Course}$

**Exercise 1.** Find an interpretation such that each concept is non-empty.

**Exercise 2.** Find out if the following concepts are satisfiable:

1.  $\text{Student} \sqcap \text{Teacher}$
2.  $\text{Student} \sqcap \text{Assistant}$

**Exercise 3.** Prove that  $\exists \text{hasDegree}.\text{Degree} \sqsubseteq \text{Person}$ .